

# Pseudopotentials reach for the stars

Gareth Conduit

TCM Group, Department of Physics

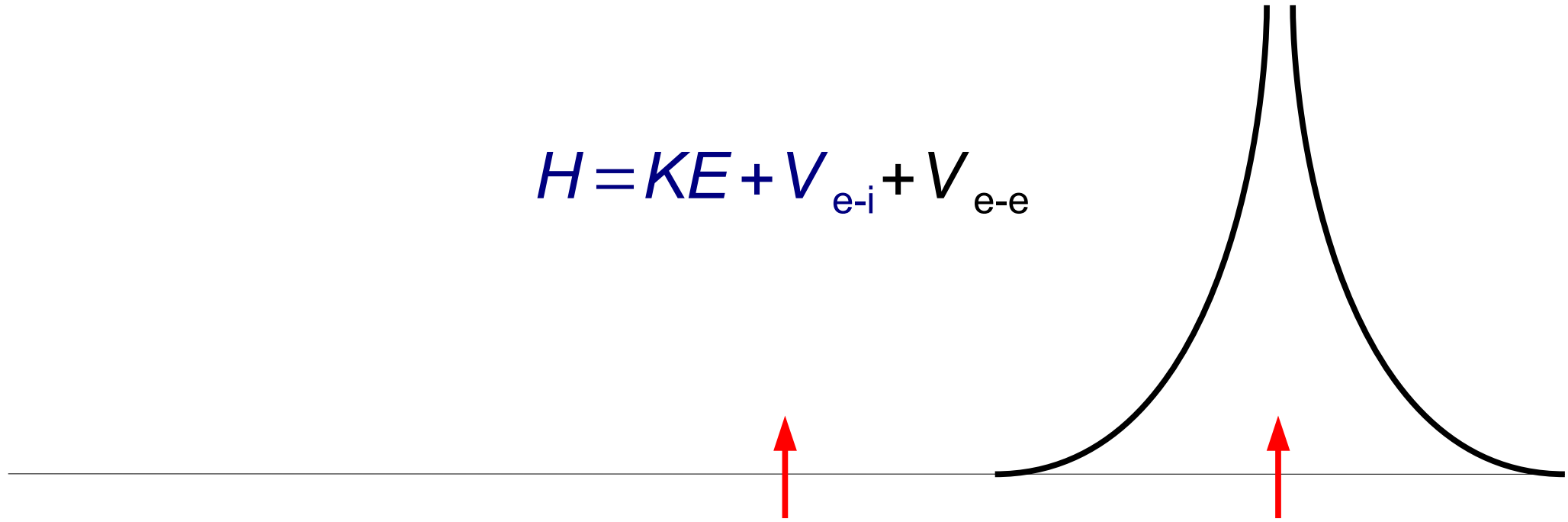
# Pseudopotential for atoms

$$H = KE + V_{e-i} + V_{e-e}$$



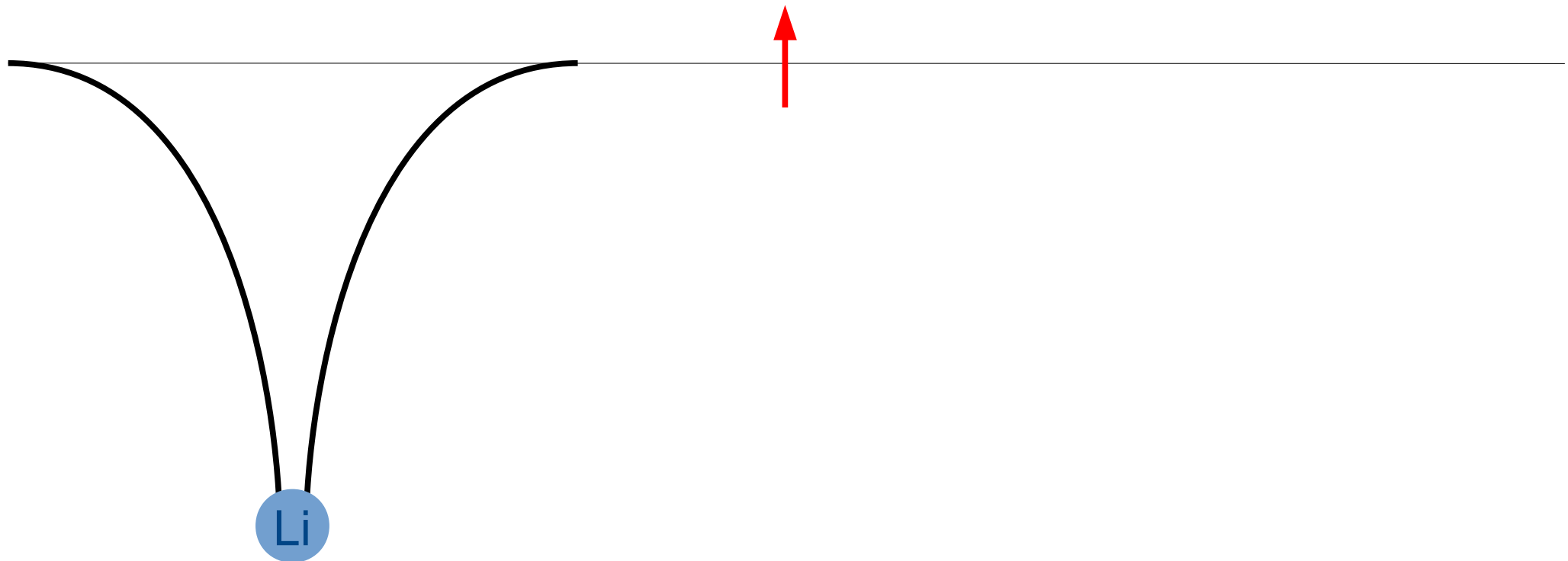
# Pseudopotential for atoms

$$H = KE + V_{e-i} + V_{e-e}$$

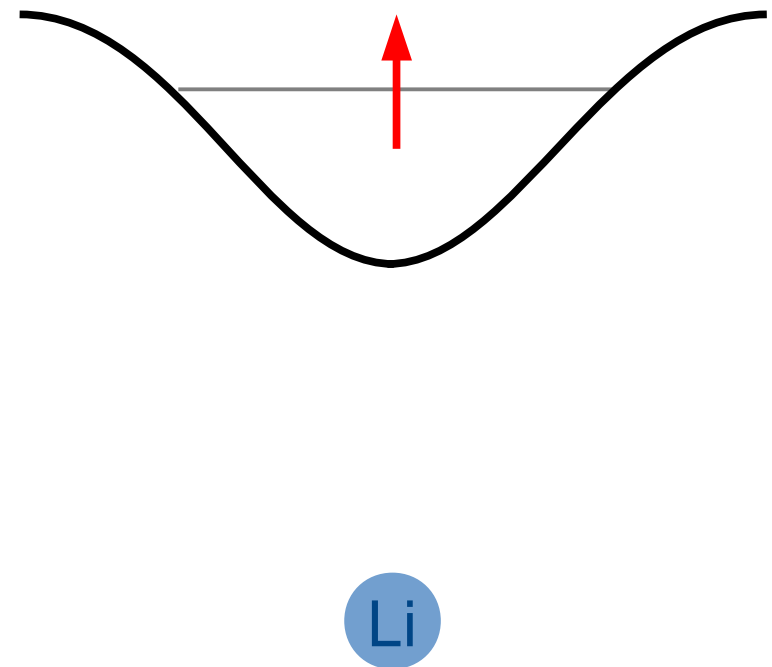
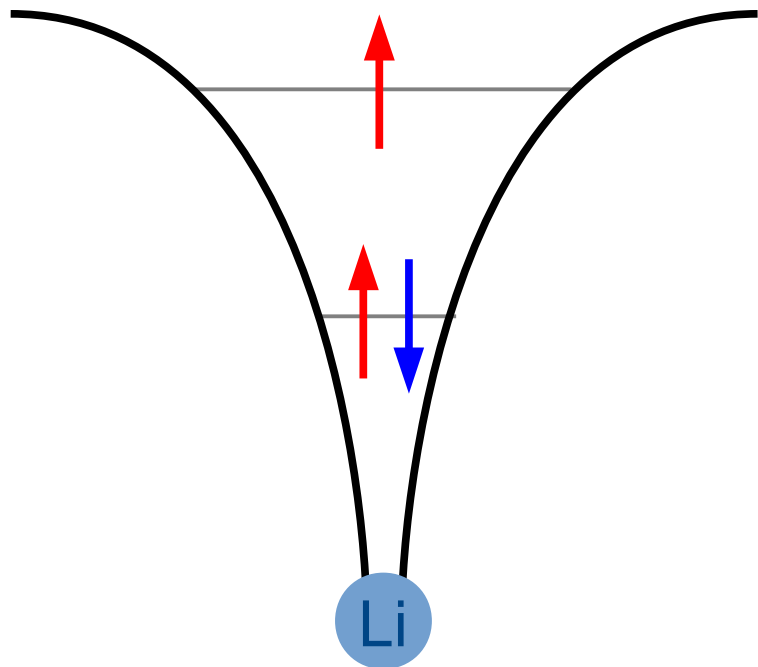


# Pseudopotential for atoms

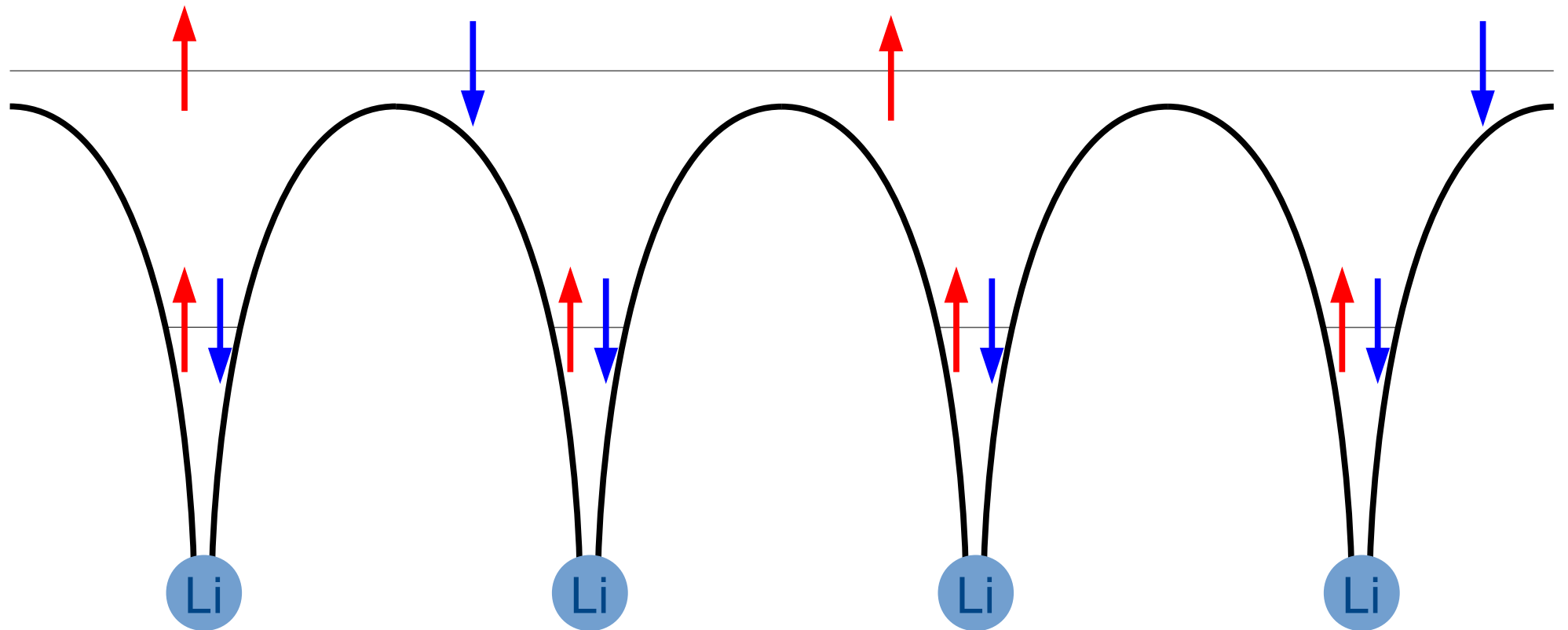
$$H = KE + V_{e-i} + V_{e-e}$$



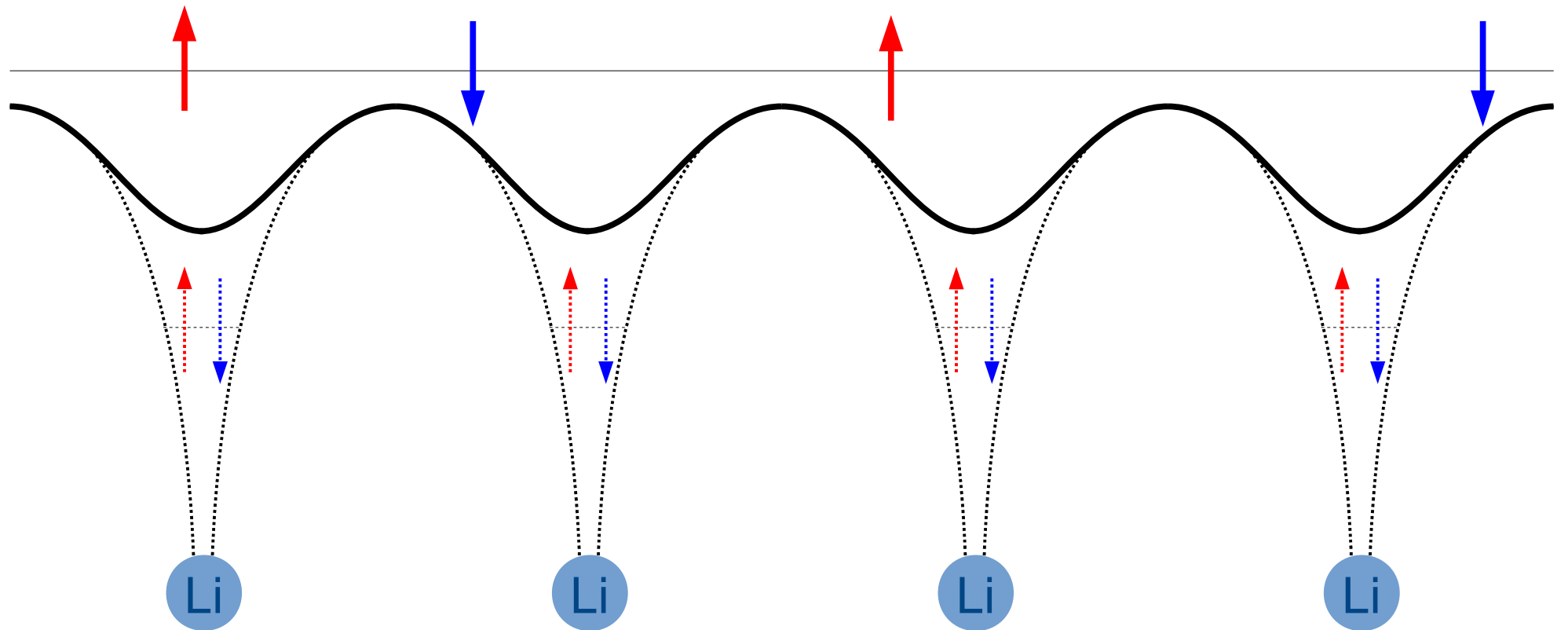
# Pseudopotential for a single atom



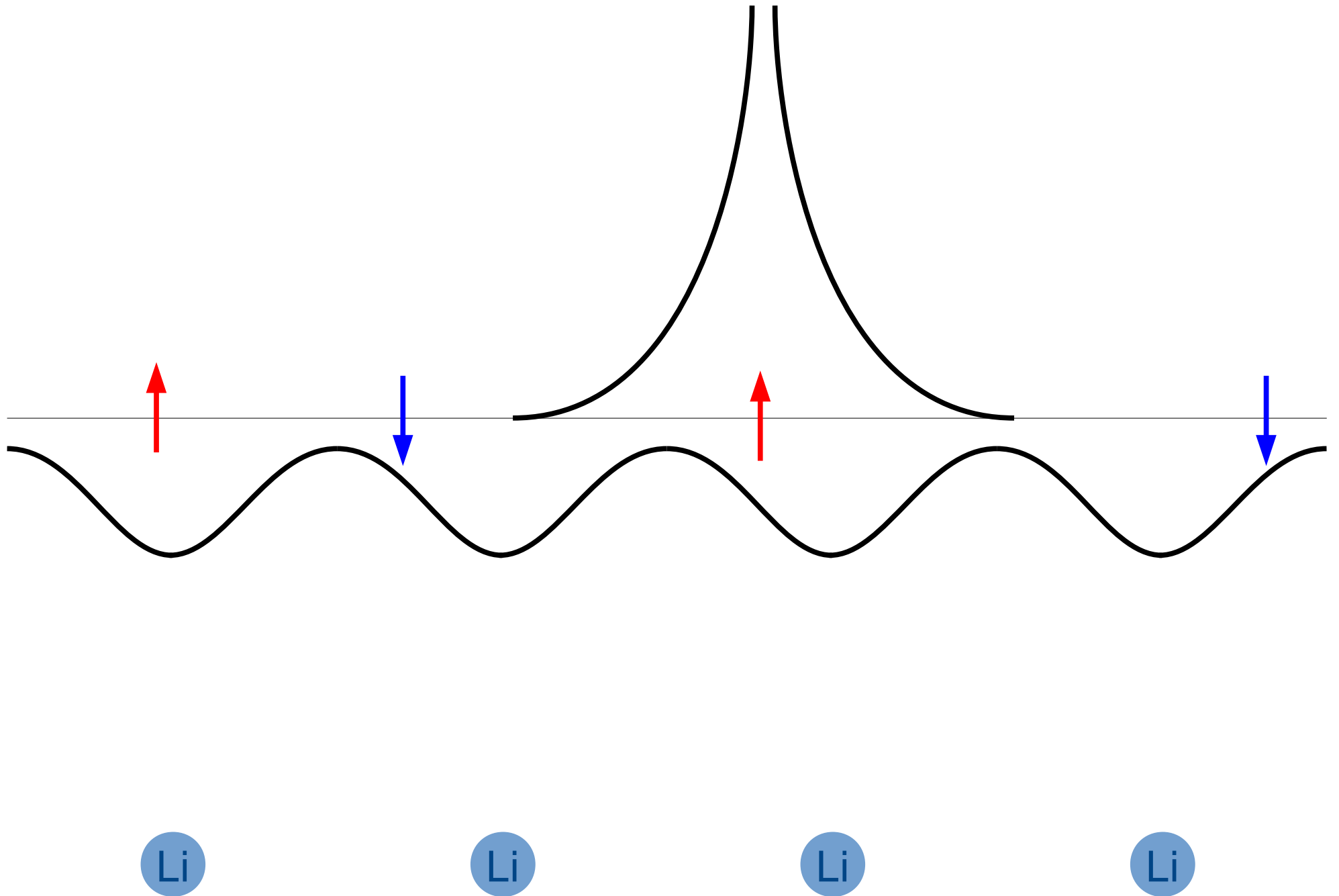
# Pseudopotential for atoms



# Pseudopotential for atoms

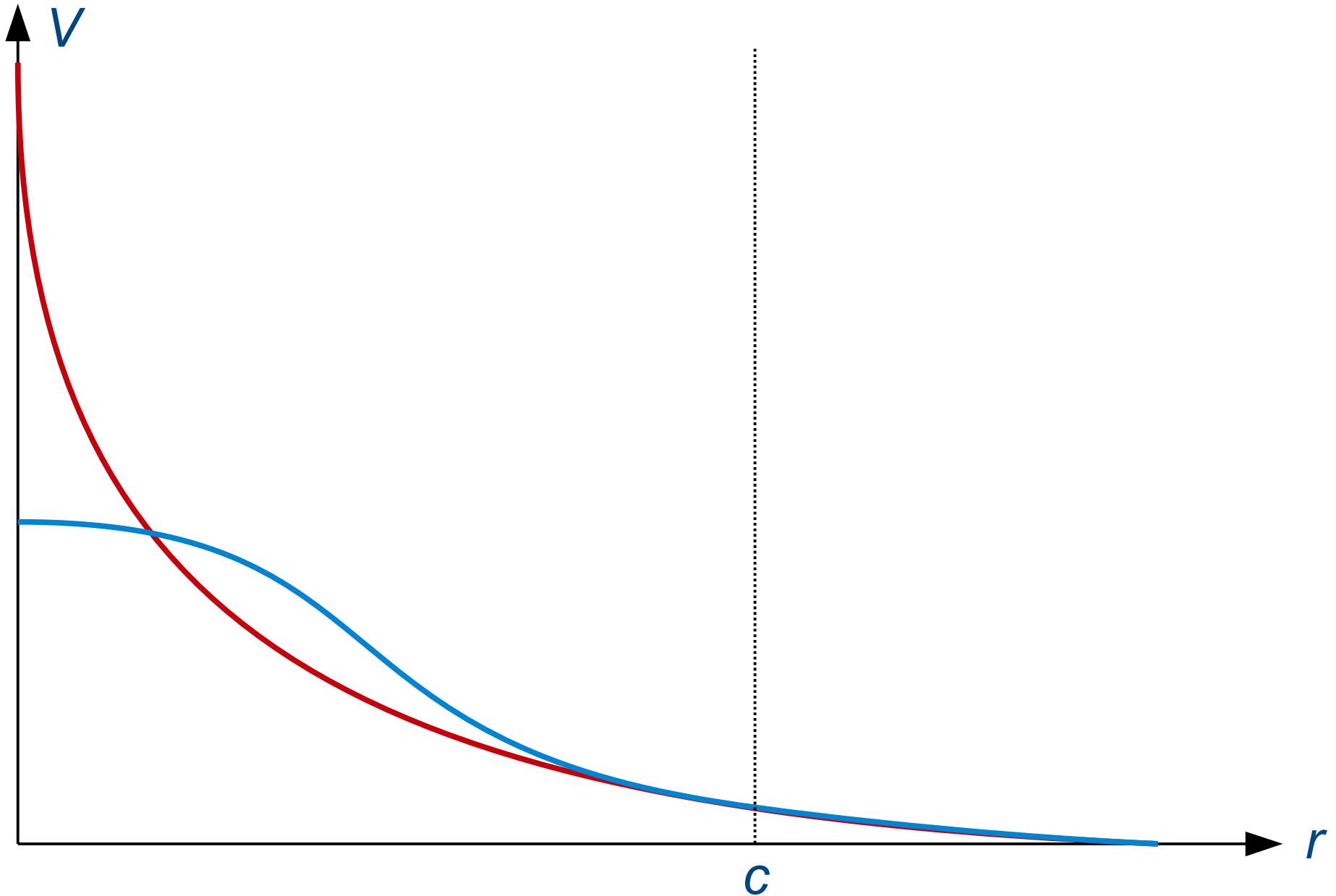


# Pseudopotential for atoms

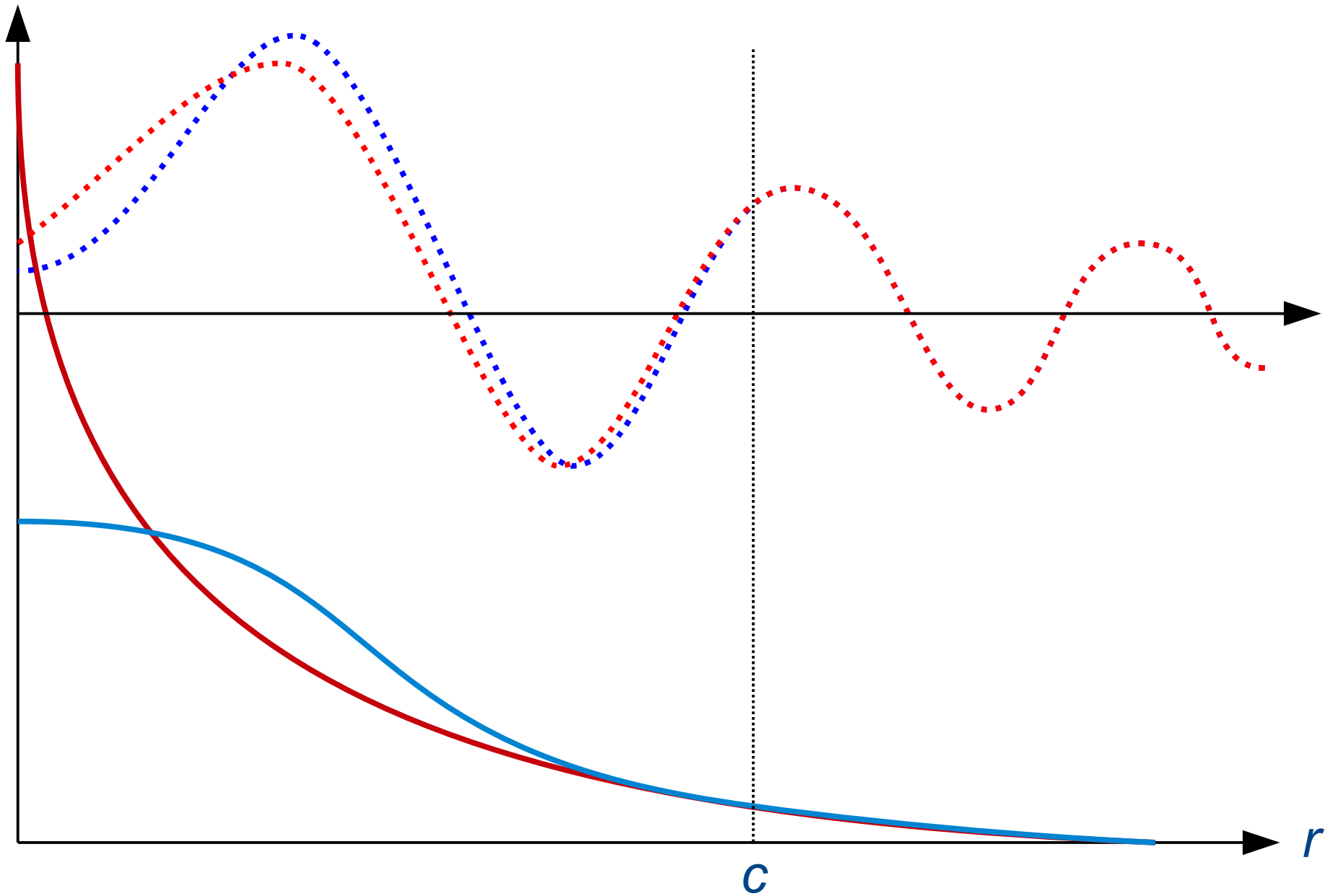




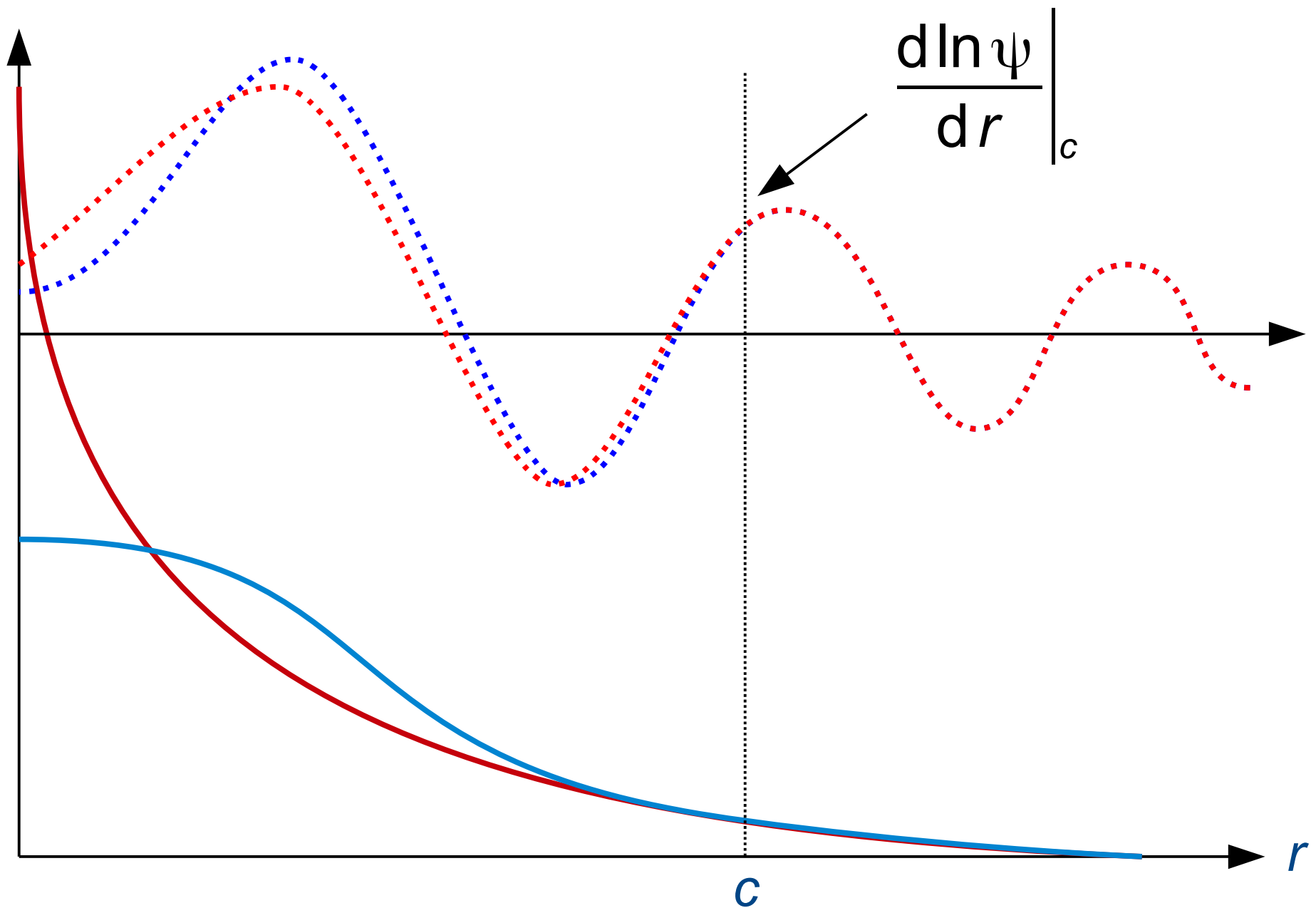
# Construction of a pseudopotential



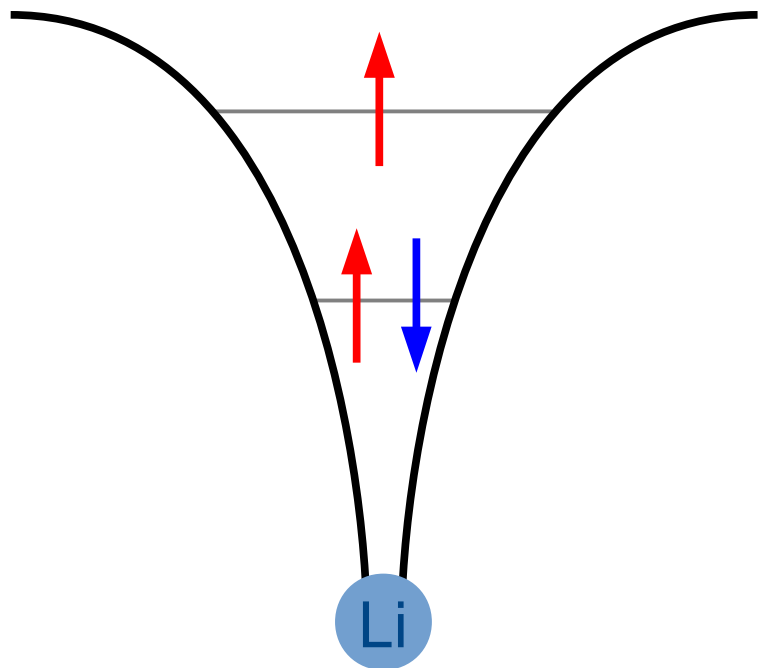
# Construction of a pseudopotential



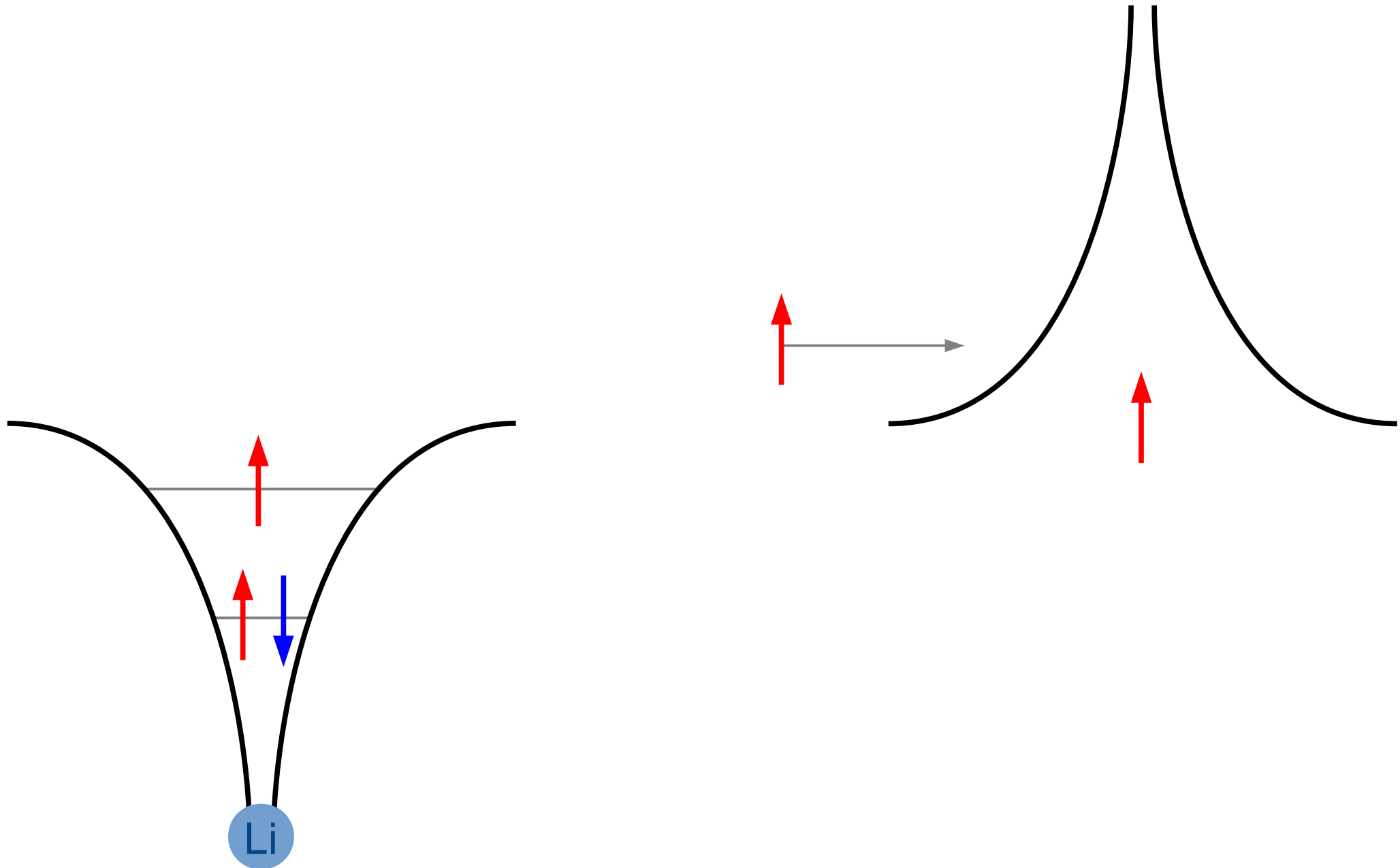
# Construction of a pseudopotential



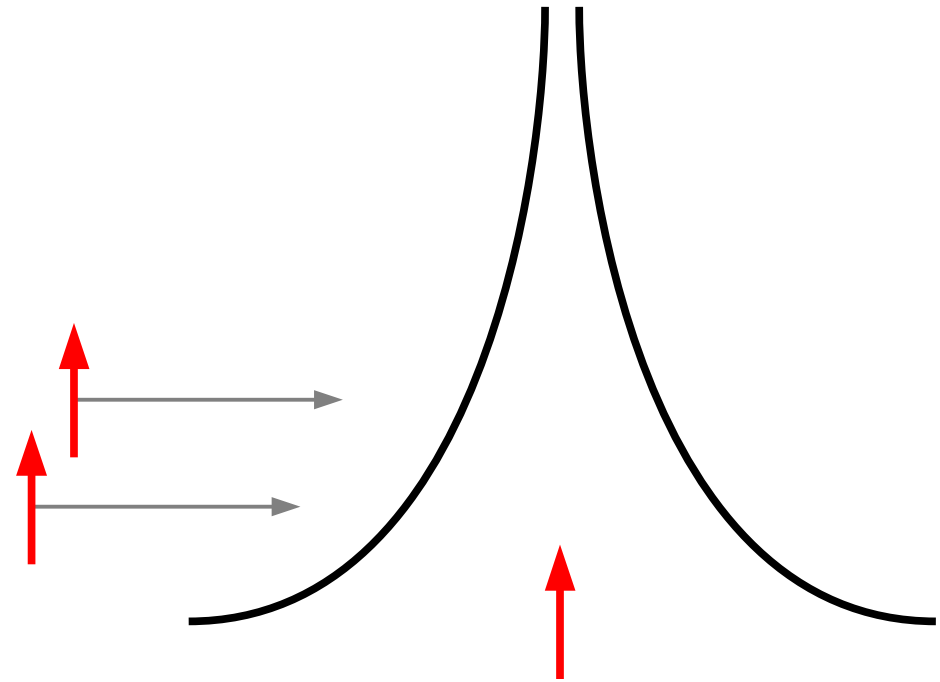
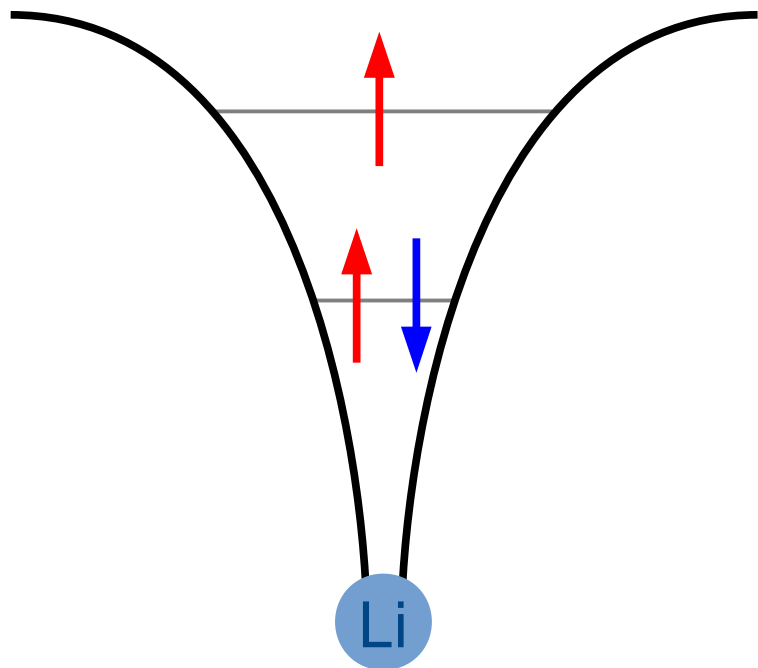
# Pseudopotential atoms vs. electrons



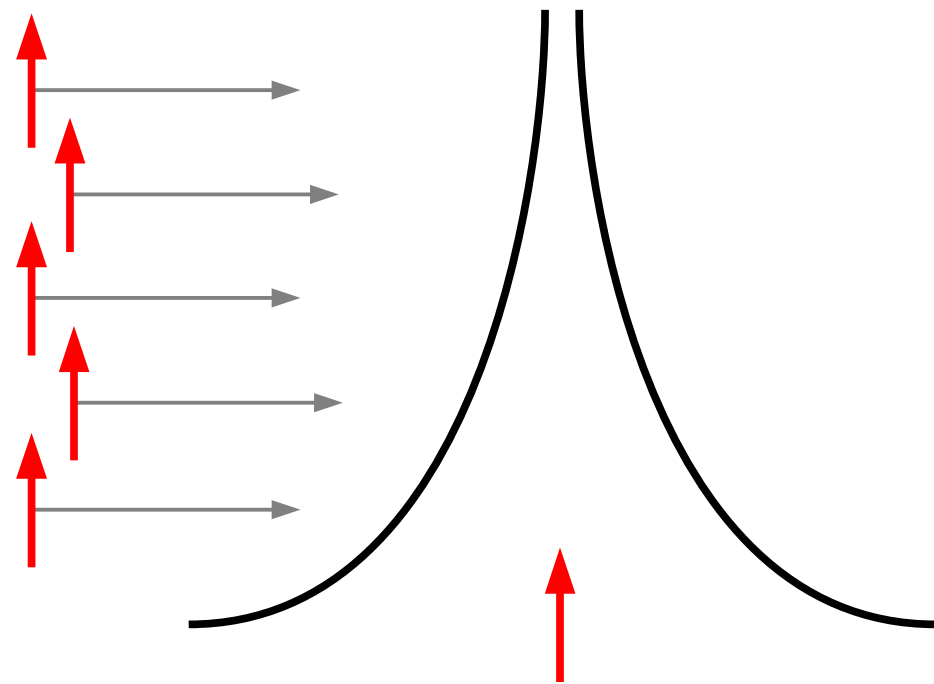
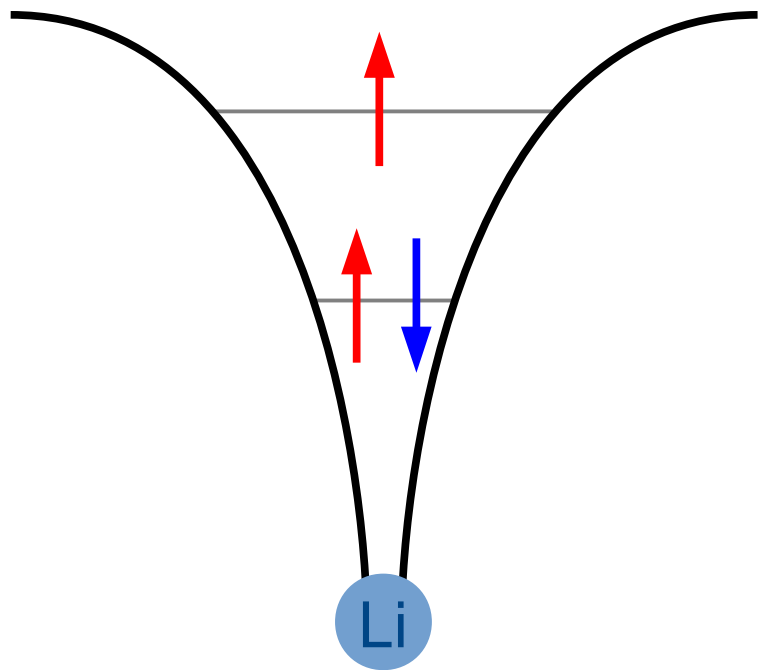
# Pseudopotential atoms vs. electrons



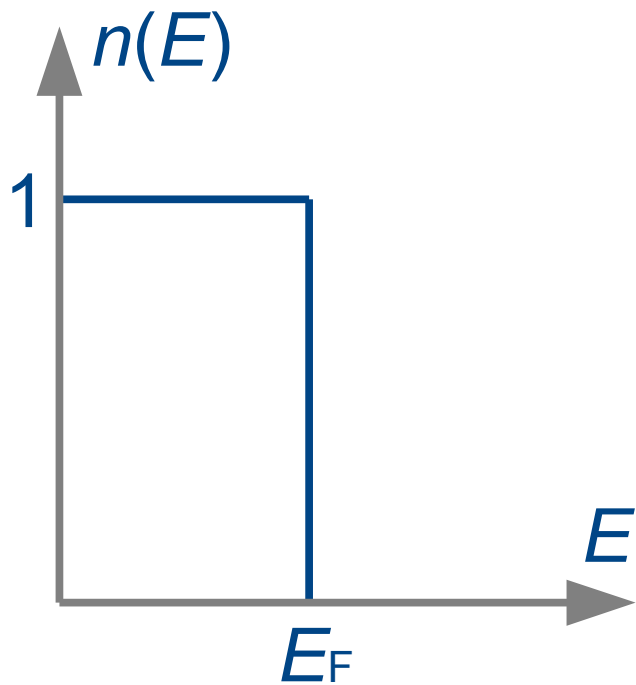
# Pseudopotential atoms vs. electrons



# Pseudopotential atoms vs. electrons



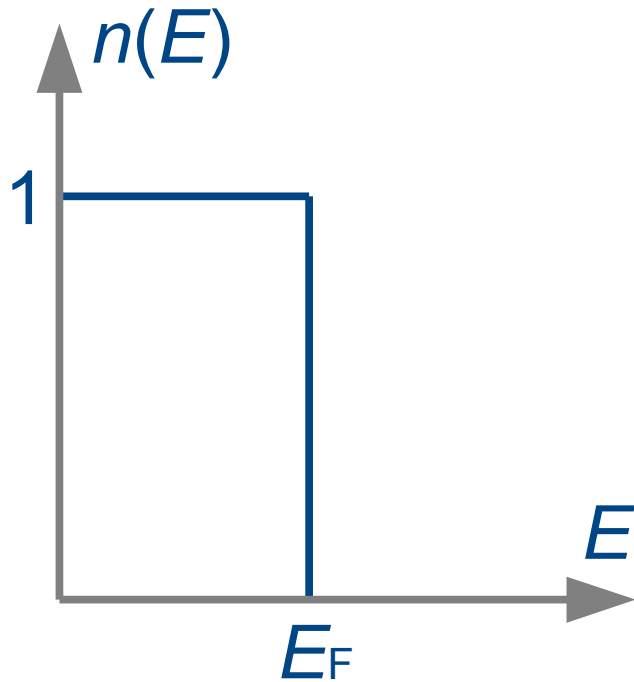
# Fermi's two ideas



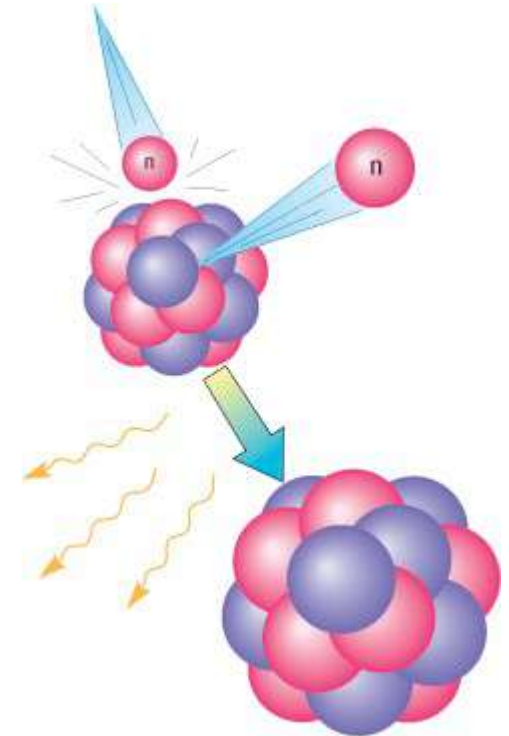
Fermi  
surface



# Fermi's two ideas



Fermi  
surface



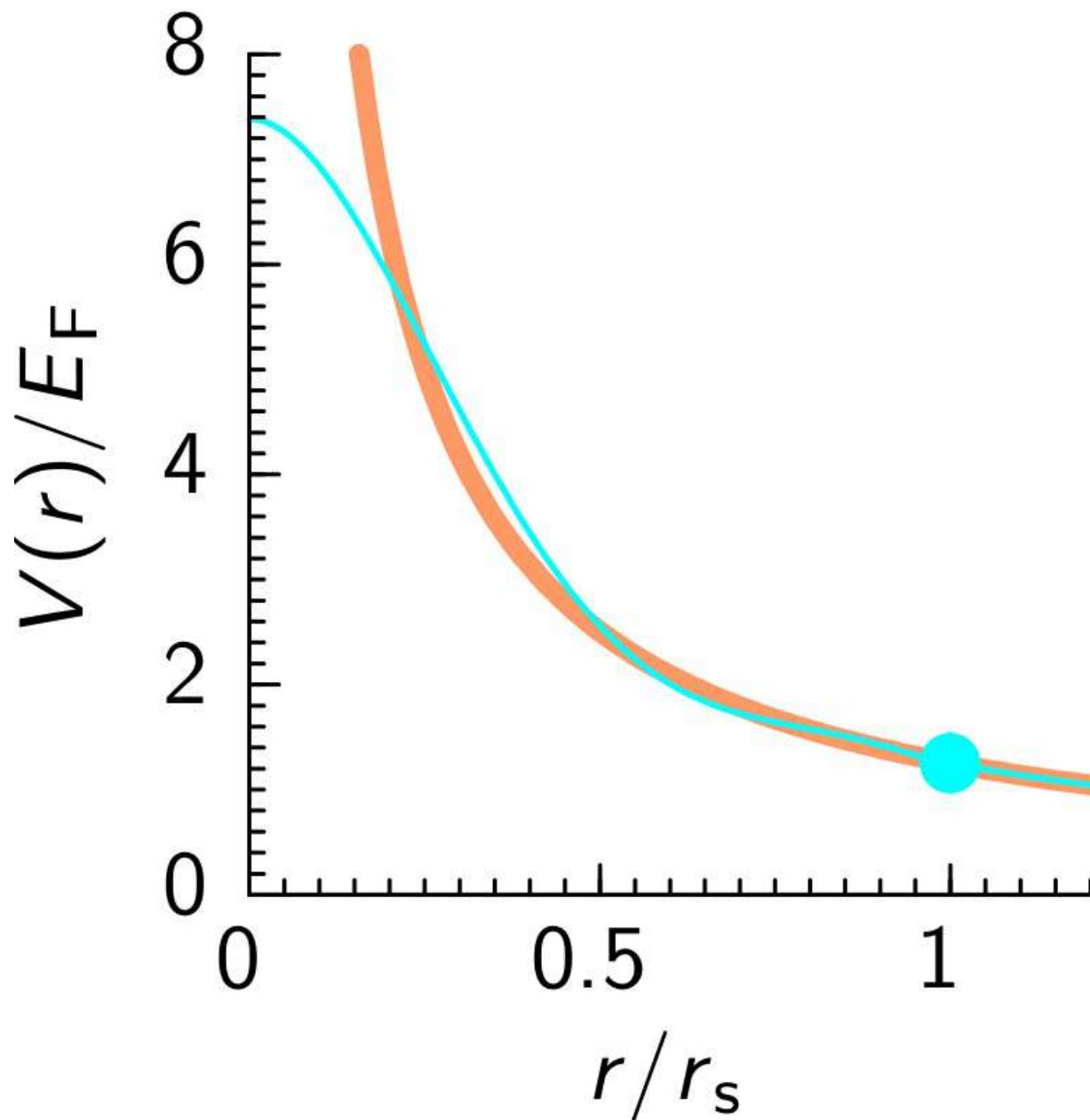
Pseudopotential for  
neutron scattering

# Construction of a pseudopotential

$$V_{\text{PP}}(r) = \begin{cases} \frac{1}{c} + \left(1 - \frac{r}{c}\right)^2 \left[ v_1 \left(\frac{1}{2} + \frac{r}{c}\right) + \sum_{i=2}^{N_v} v_i \left(\frac{r}{c}\right)^i \right] & r < c \\ \frac{1}{r} & r > c \end{cases}$$

$$\sum_{l=0}^{l_{\max}} \int_0^{2k_F} dk \left[ \left. \frac{d \ln \psi_{\text{PP}}(k, l)}{dr} \right|_c - \left. \frac{d \ln \psi_{\text{Coul}}(k, l)}{dr} \right|_c \right]^2$$

# Pseudopotential



# Quantum Monte Carlo

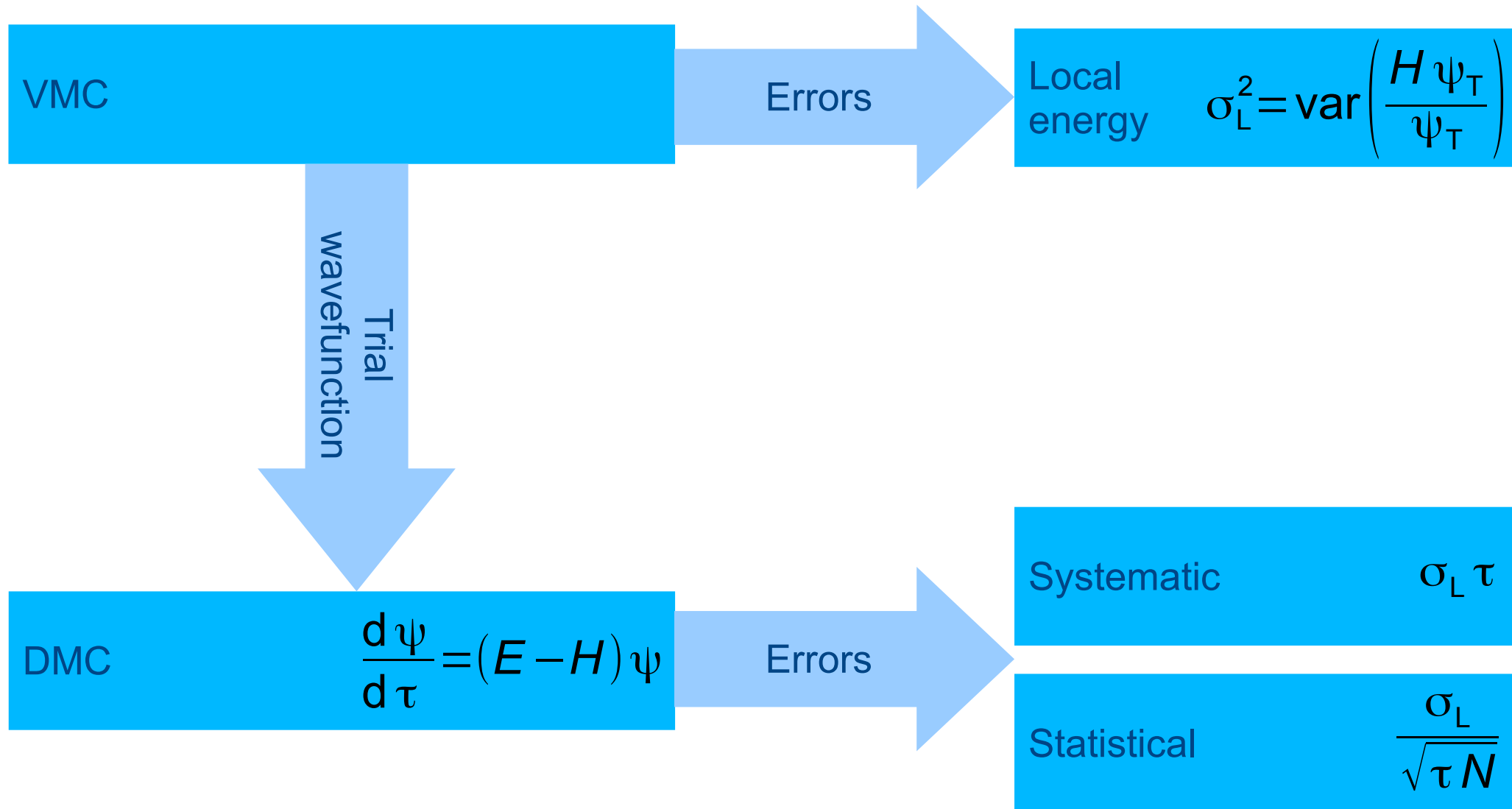
VMC

Errors

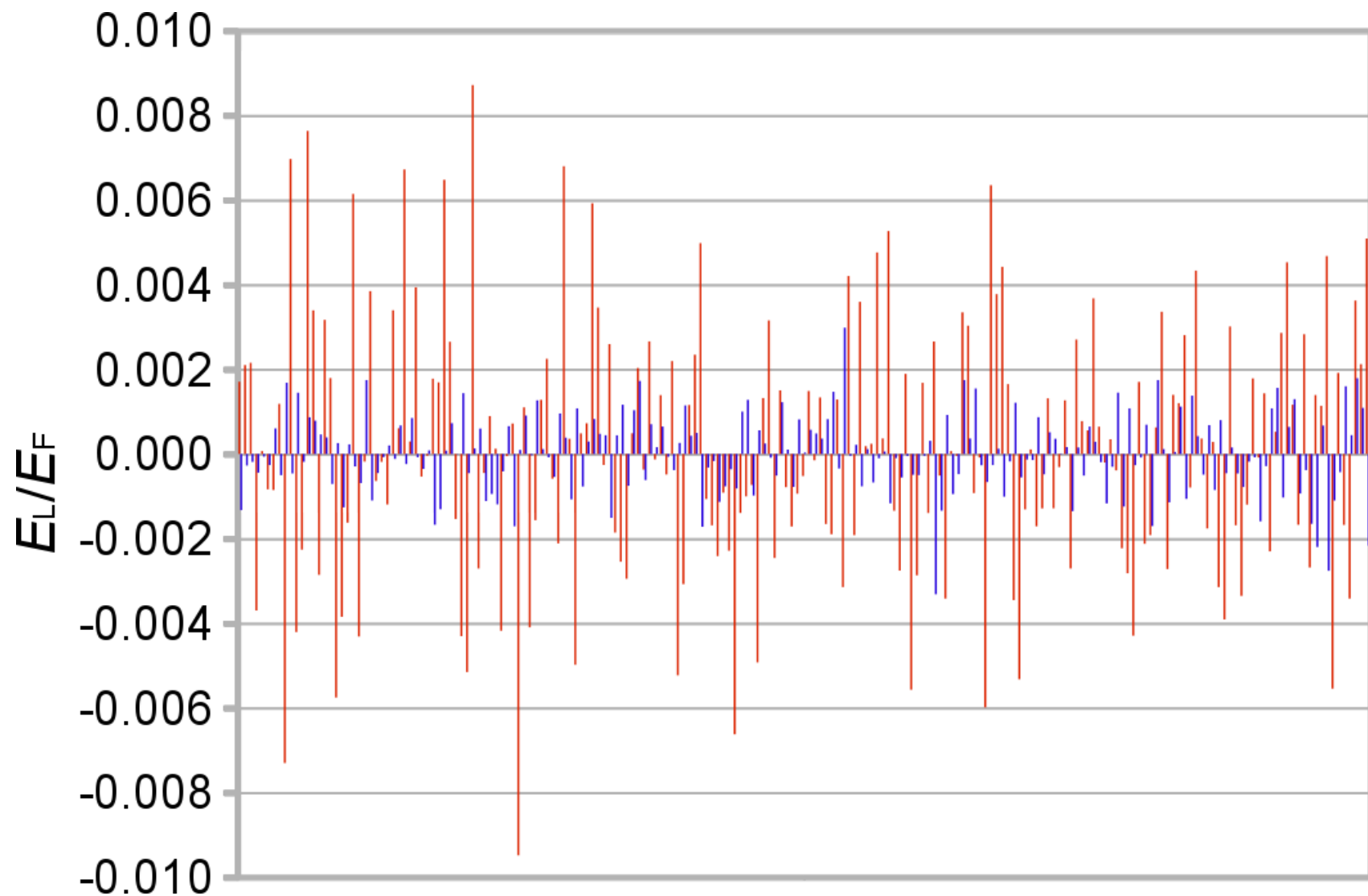
Local  
energy

$$\sigma_L^2 = \text{var} \left( \frac{H \psi_T}{\psi_T} \right)$$

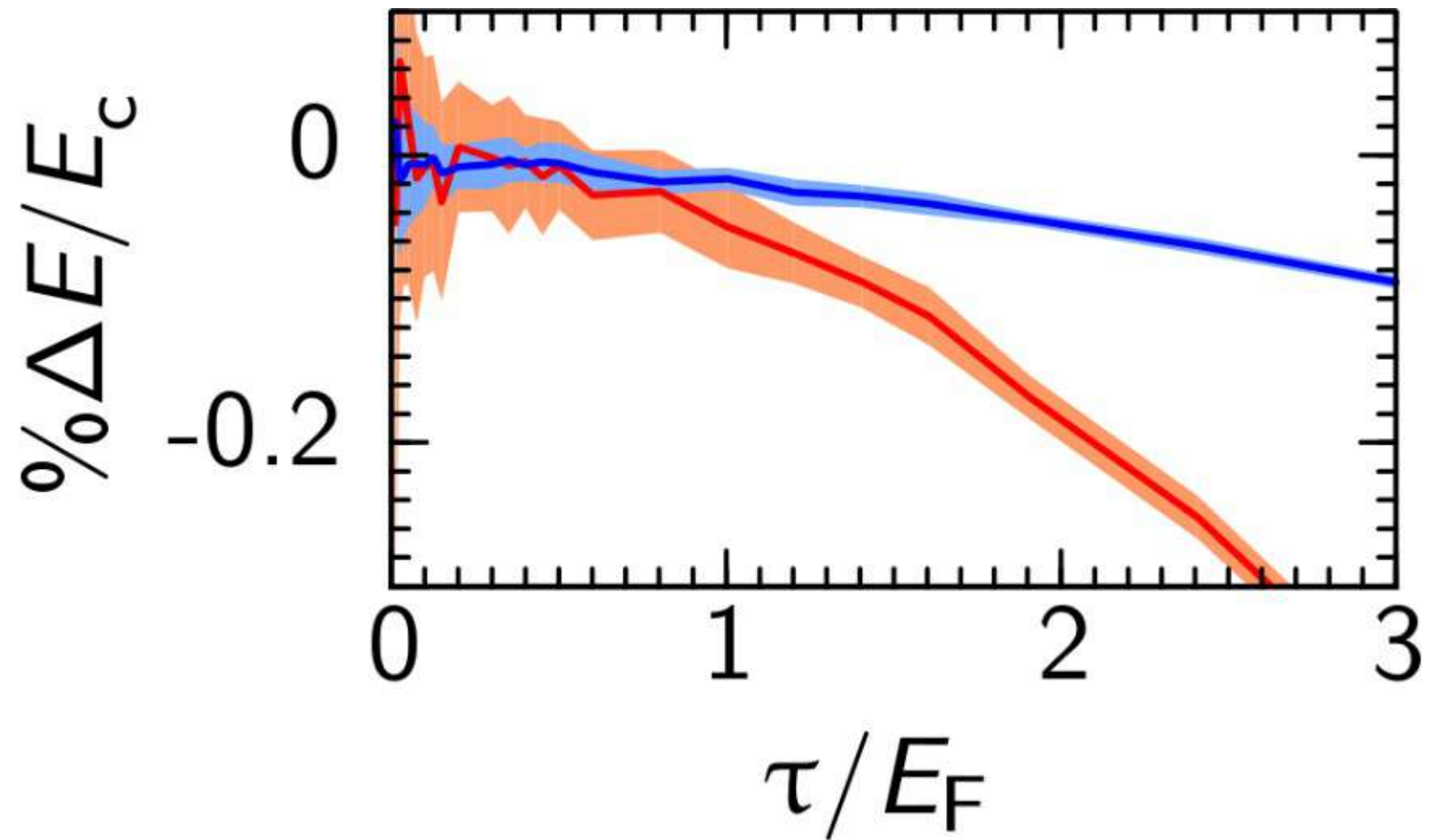
# Quantum Monte Carlo



# Pseudopotential: local energy



# Pseudopotential: time step

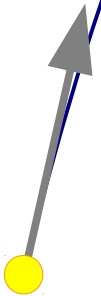
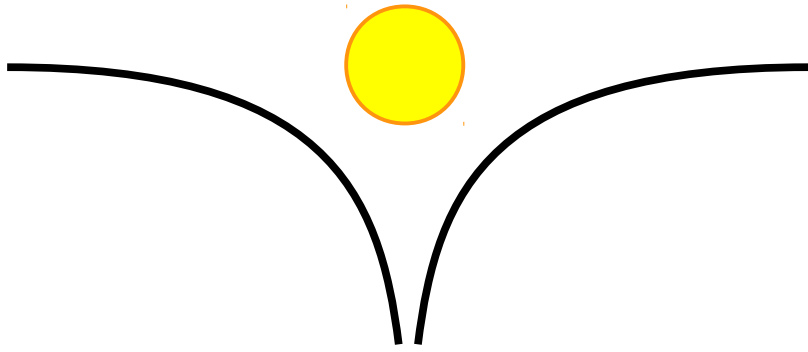


# Galactic dynamics

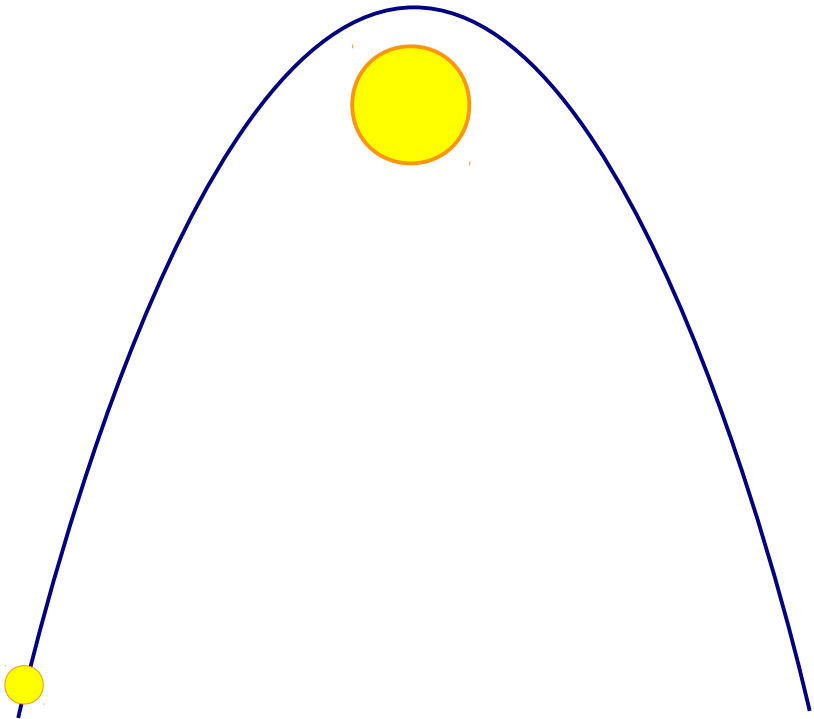
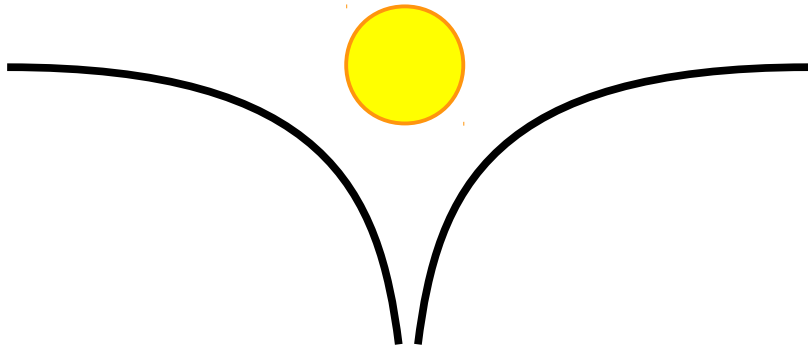




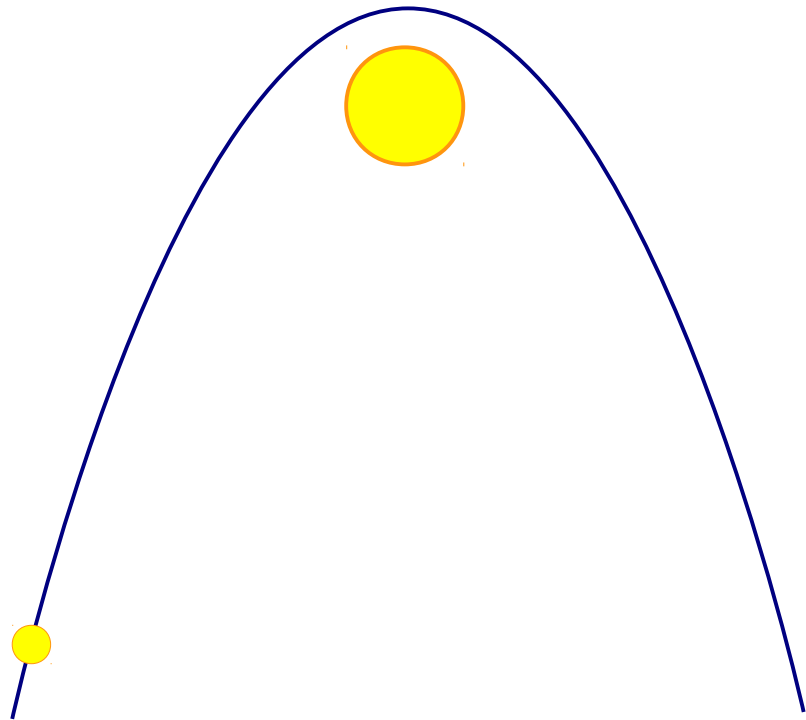
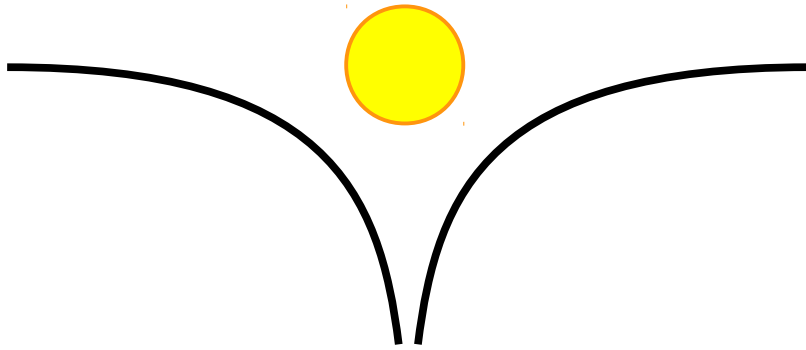
# Galactic dynamics



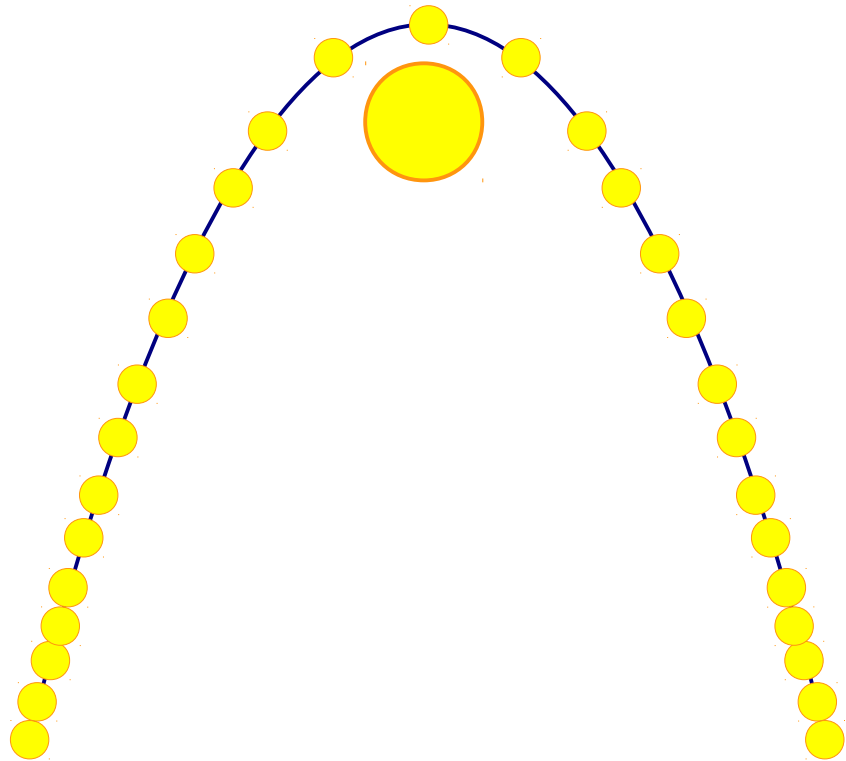
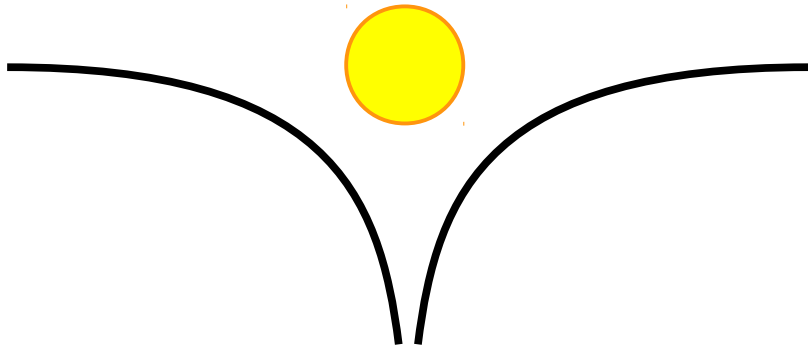
# Galactic dynamics



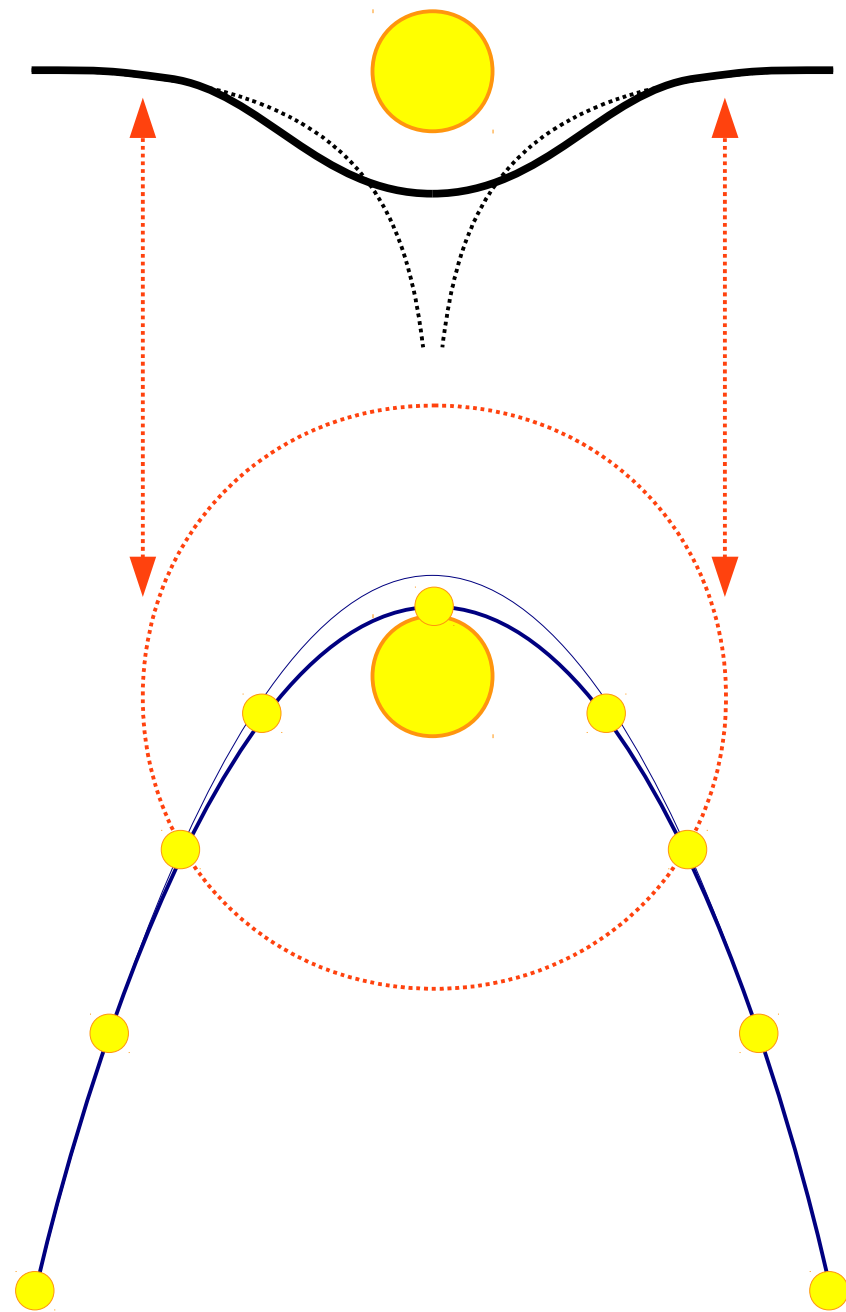
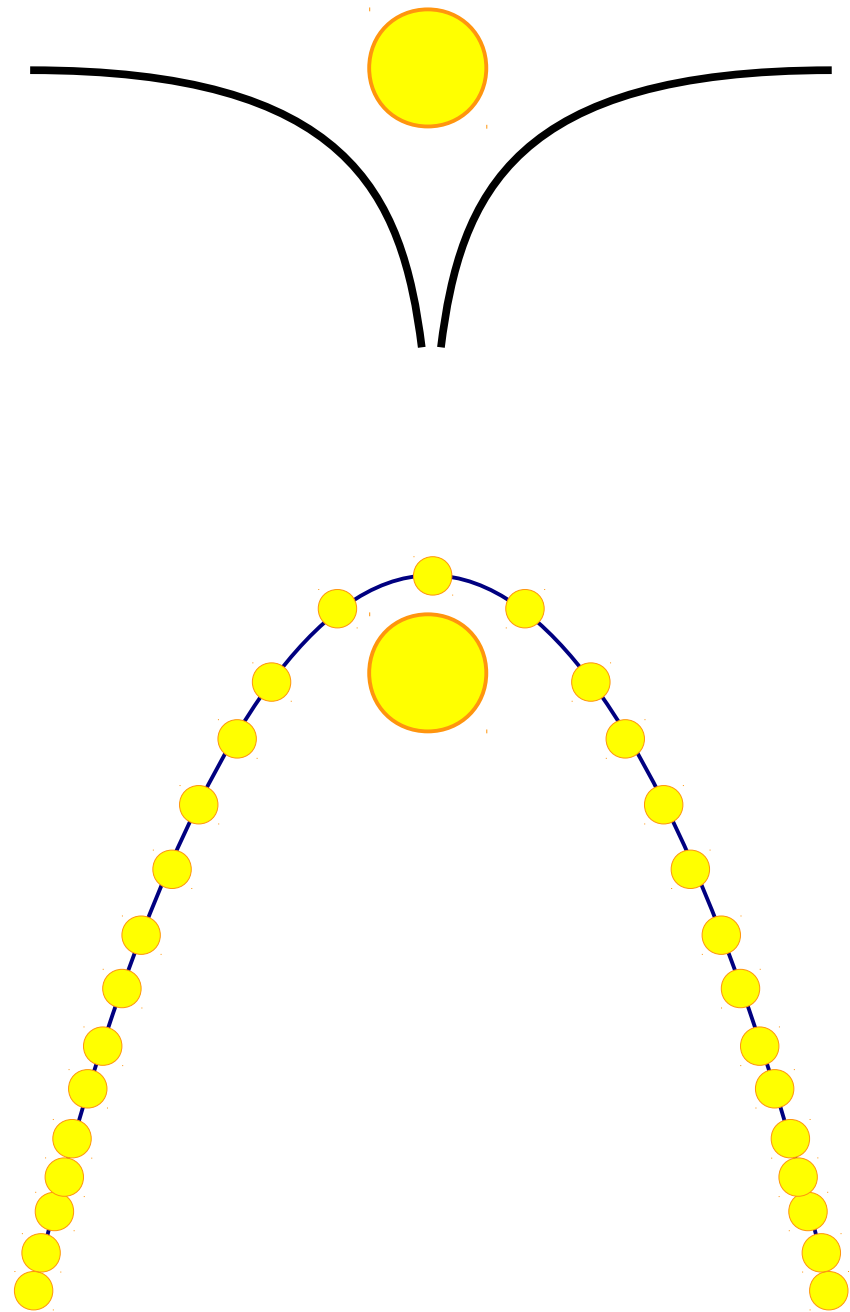
# Galactic dynamics



# Galactic dynamics



# Galactic dynamics



# Summary

Developed a pseudopotential for the repulsive Coulomb interaction

Accelerates numerical calculations by a factor of 30

Pseudopotentials could be applied to cold atoms contact interaction and galactic dynamics