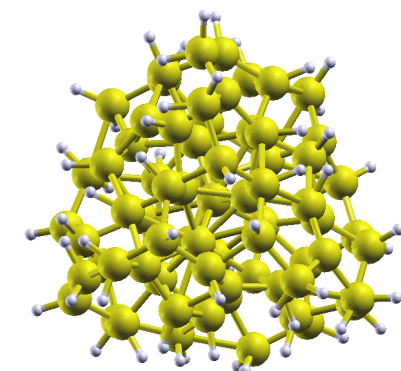
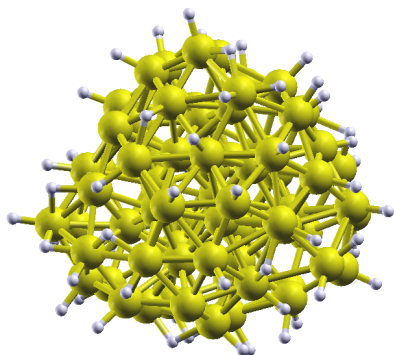


# Pressure-induced structural transformations in nanomaterials: a linear-scaling DFT investigation

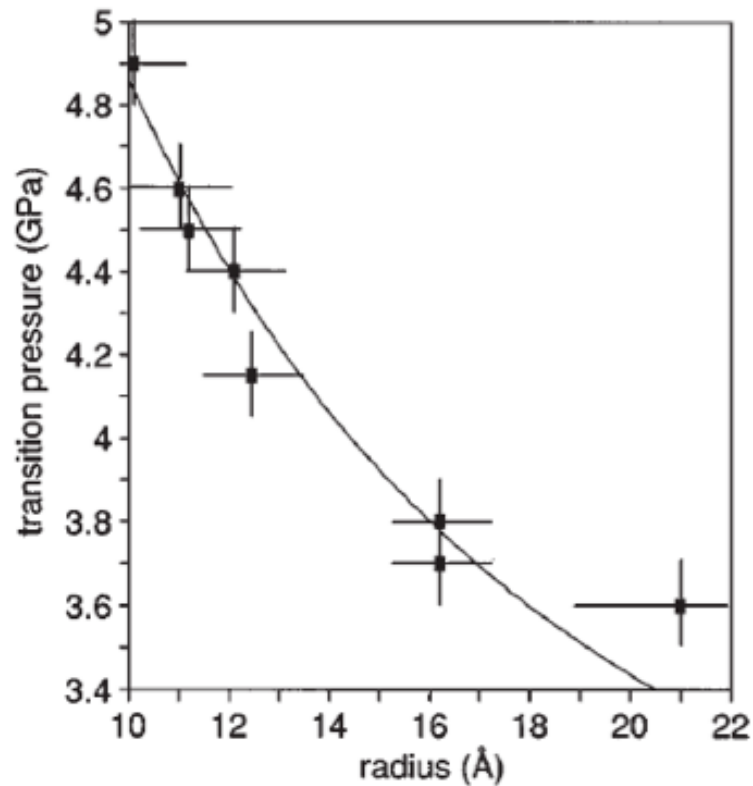
Niccolò Corsini<sup>1</sup>, Peter Haynes<sup>1</sup>, Carla Molteni<sup>2</sup> & Nicholas Hine<sup>3</sup>  
Imperial College London<sup>1</sup>, King's College London<sup>2</sup> & Cambridge University<sup>3</sup>



Available on J. Chem. Phys. **139**, 084117 (2013)

# Motivation

- Nanocrystal **size and surface** add extra dimensions to phase diagram

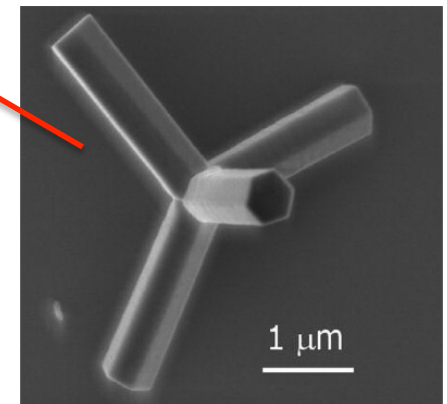
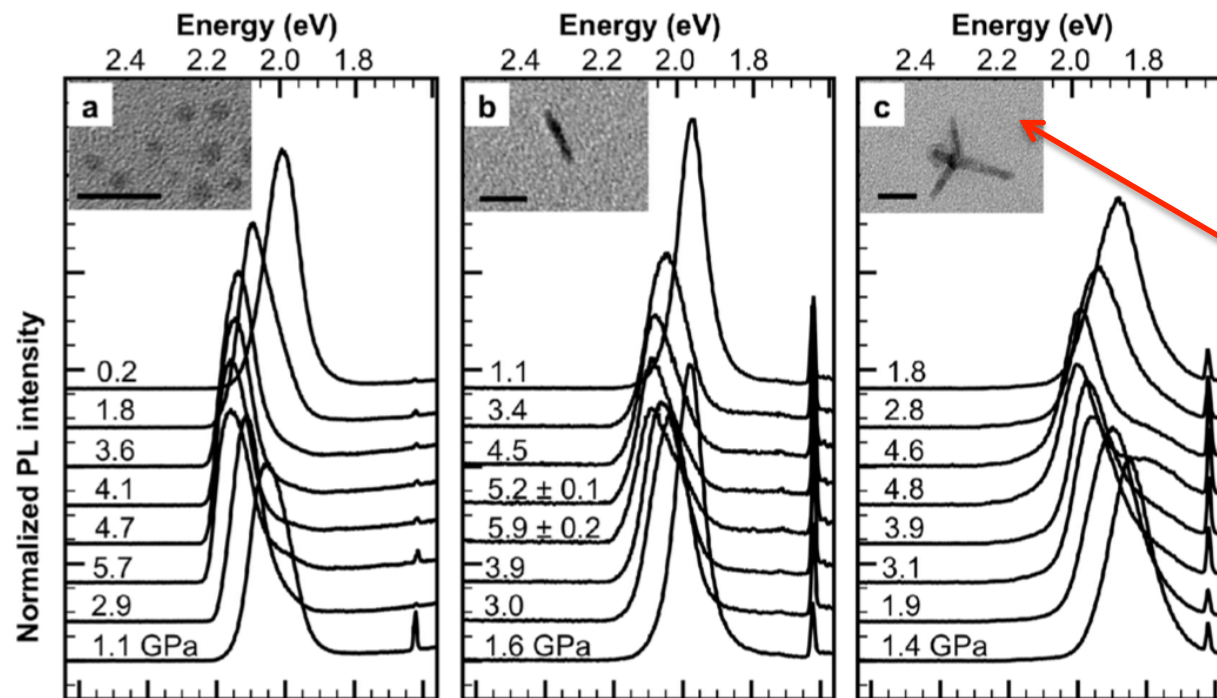


← CdSe WZ/RS nanocrystals

# Motivation

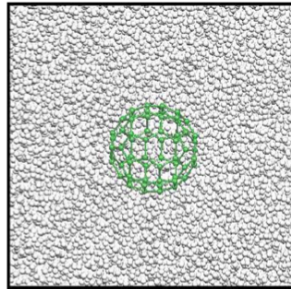
- Nanocrystal size and surface add extra dimensions to phase diagram
- **Ideal model** for kinetics of solid-solid **transformation**
- CdSe/CdS nanocrystal display **tunable** optical properties
- Can use as nanoscale **pressure sensors**

CdS/CdSe dots, rods & tetrapods

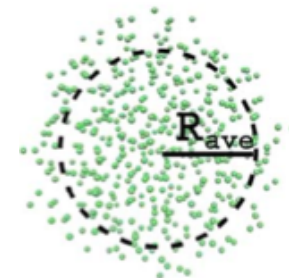
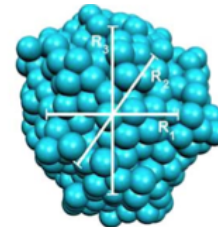
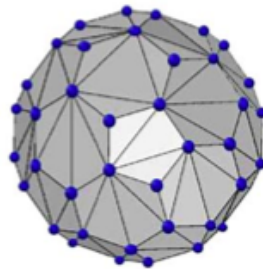
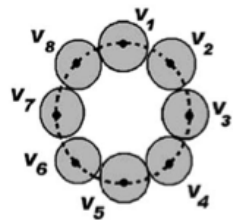


# Finite systems under pressure

- Two approaches for finite systems :
  - 1) **Explicitly** describing the pressure transmitting **solvent**



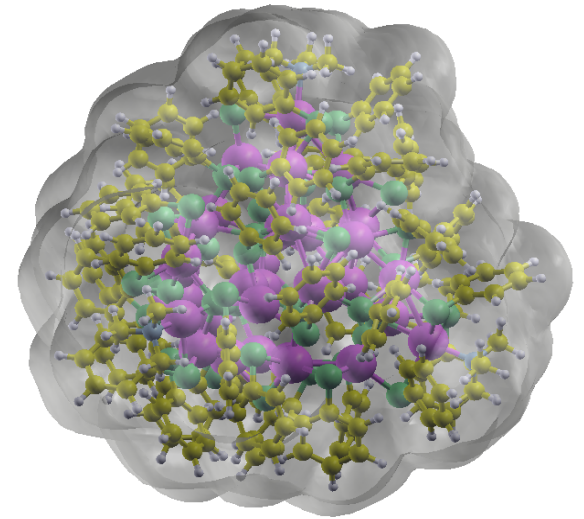
- 2) Introduce a **PV term** after defining volume as a function of **atomic coordinates**



**NON PERIODICITY => V DEFINITION NOT UNIQUE**

# Electronic enthalpy method

- Natural to use **electronic density** to define **volume** of complex structures
- DFT self-consistent minimization of enthalpy  $H$



$$H[\rho] = U[\rho] + PV_e[\rho]$$

- **Electronic volume** defined as the interior of a **charge isosurface** of  $\alpha$  density cutoff value

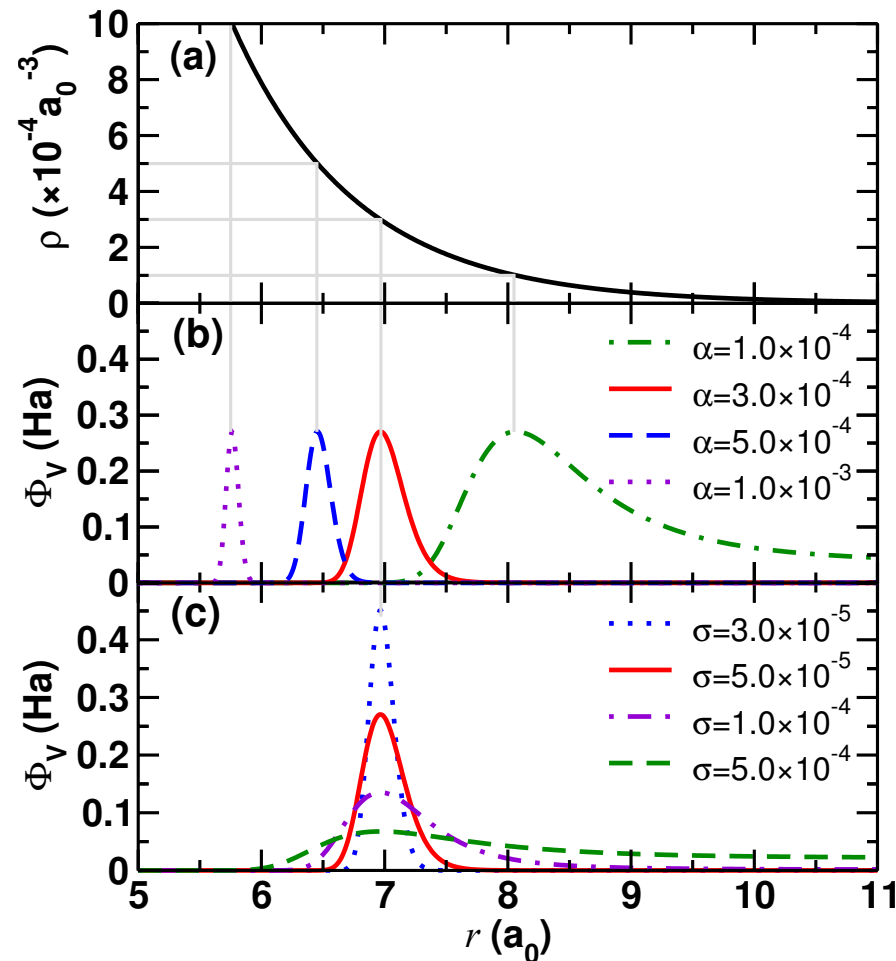
$$V_e = \int \theta(\rho(\mathbf{r}) - \alpha) dr^3$$

- Step function is smeared by  $\sigma$  for numerical reasons

# Advantages

- Potential contribution due to PV is **simple**

$$\Phi_V(r) = P \frac{\delta V_e}{\delta \rho} \Big|_{\rho=\rho(r)} = \frac{P}{\sigma \sqrt{2\pi}} \exp\left(-\frac{(\rho(\mathbf{r}) - \alpha)^2}{2\sigma^2}\right)$$

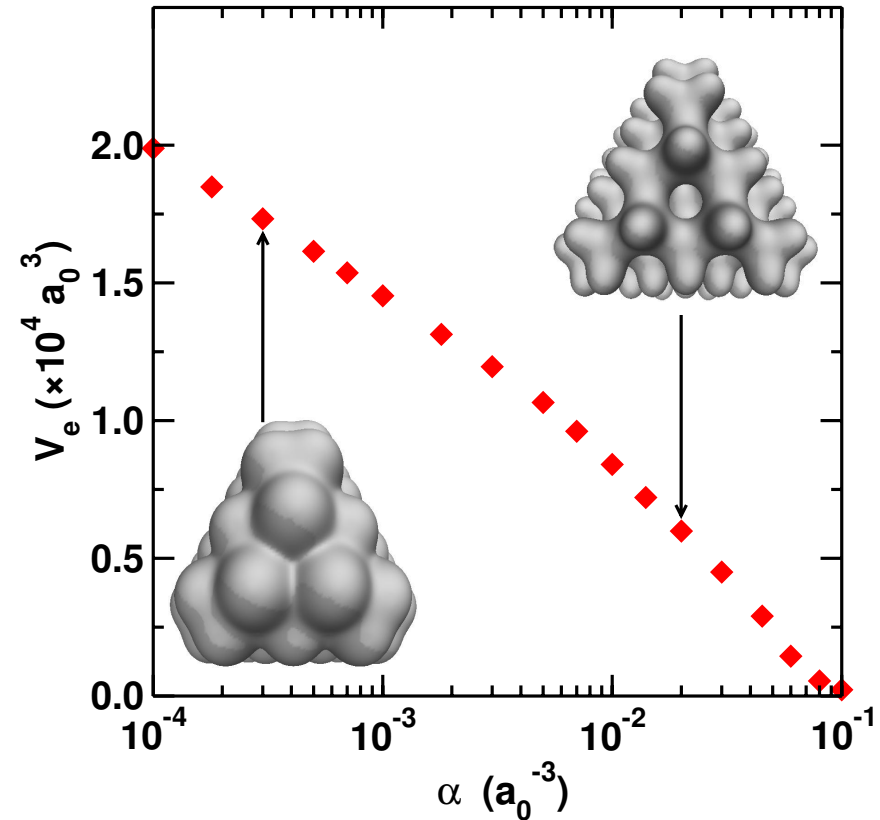
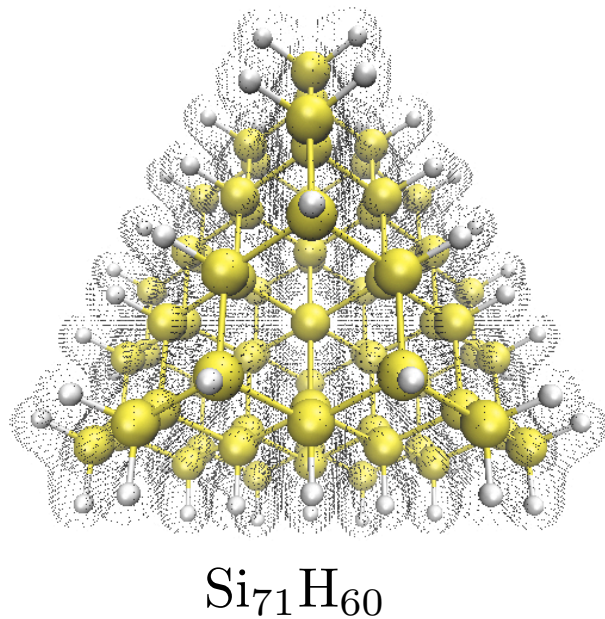


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$$\Phi_V(r) = P \frac{\delta V_e}{\delta \rho} \Big|_{\rho=\rho(r)} = \frac{P}{\sigma \sqrt{2\pi}} \exp\left(-\frac{(\rho(\mathbf{r}) - \alpha)^2}{2\sigma^2}\right)$$

- Pressure field acts **directly** on electrons
- **No** need for **equilibration** with pressurizing medium.
- **Efficient** compared to other *ab initio* methods
- Gives a **homogeneous description** of the solvent-nanocrystal interface with  $\alpha$  defining the excluded volume of solvent and  $\sigma$  the range/intensity of interaction

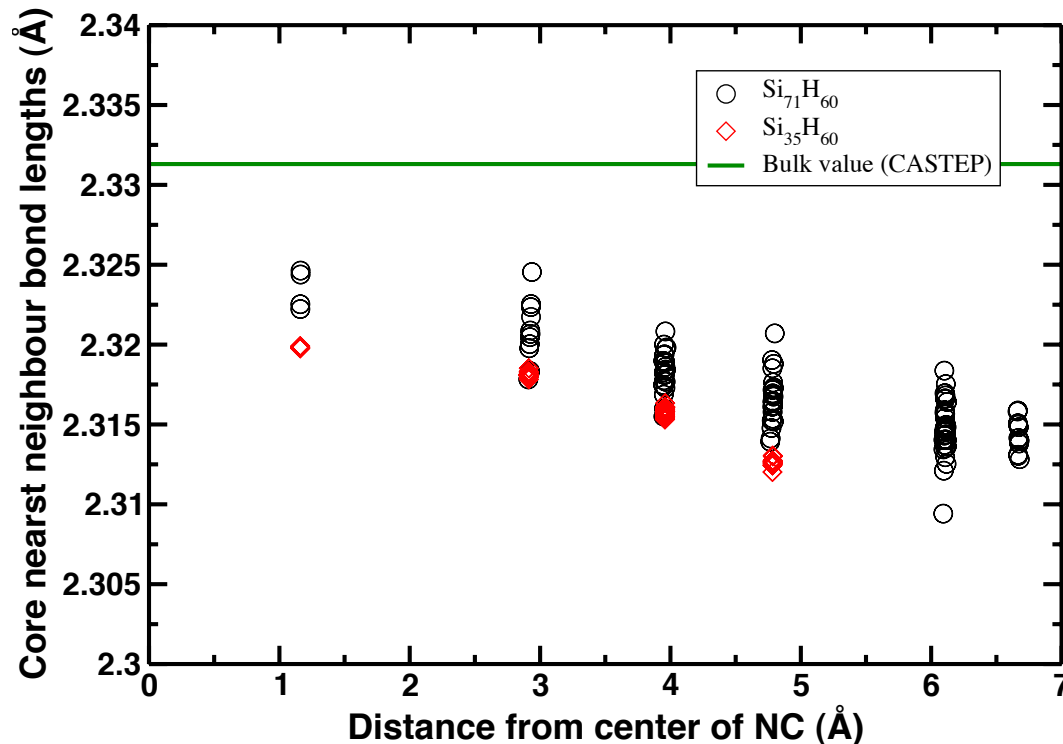


- $\alpha$  needs to be sufficiently large to avoid describing voids and **calibrated** to correspond to a **realistic excluded volume**
- $\sigma$  has to be tuned and needs to be sufficiently large for the potential to be accurately integrated on the grid



# Calibration

- If  $\alpha$  and  $\sigma$  were chosen correctly, the **effective pressure** felt inside the nanocrystal should match the input pressure
- Exploit the fact that the core has very similar bond lengths and symmetry compared to the bulk and by virtue of **nearsightedness principle** similar elastic properties



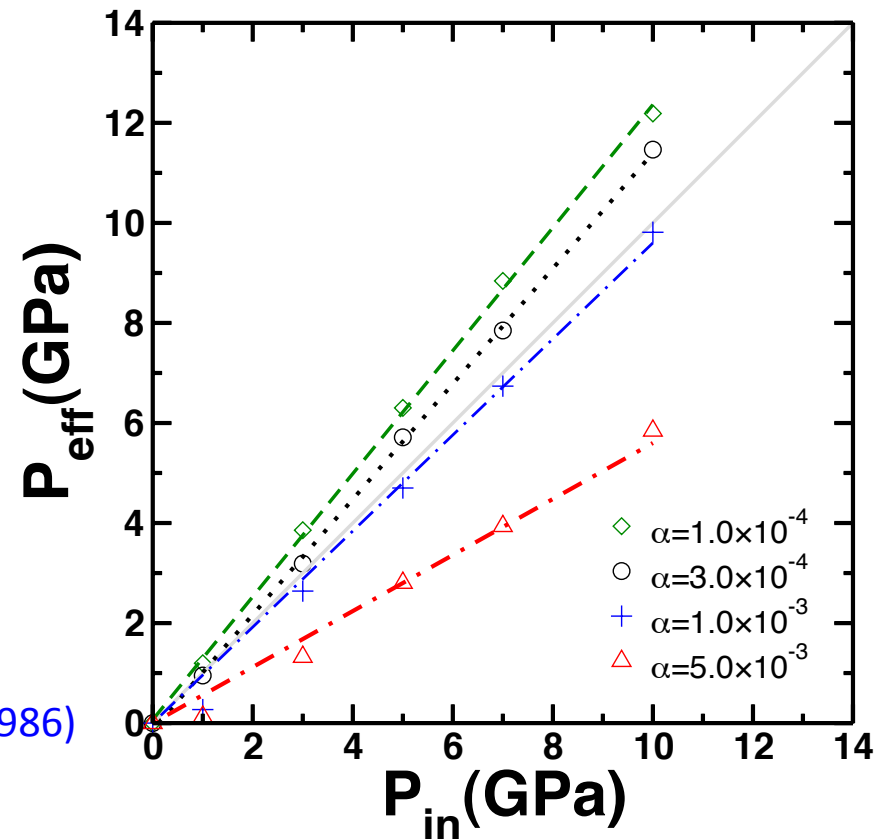
# Calibration

- **Calibration** on  $\text{Si}_{71}\text{H}_{60}$  matching the applied pressure to an **effective pressure**<sup>1</sup> estimated from the compression of bulk-like nearest neighbor bond length

$$P_{\text{eff}} = 3B_0 \left( \frac{a}{a_{\text{eq}}} \right)^{-2} \left( 1 - \frac{a}{a_{\text{eq}}} \right) \exp \left[ - \frac{3}{2} (B'_0 - 1) \left( \frac{a}{a_{\text{eq}}} - 1 \right) \right]$$

## SIMULATION DETAILS

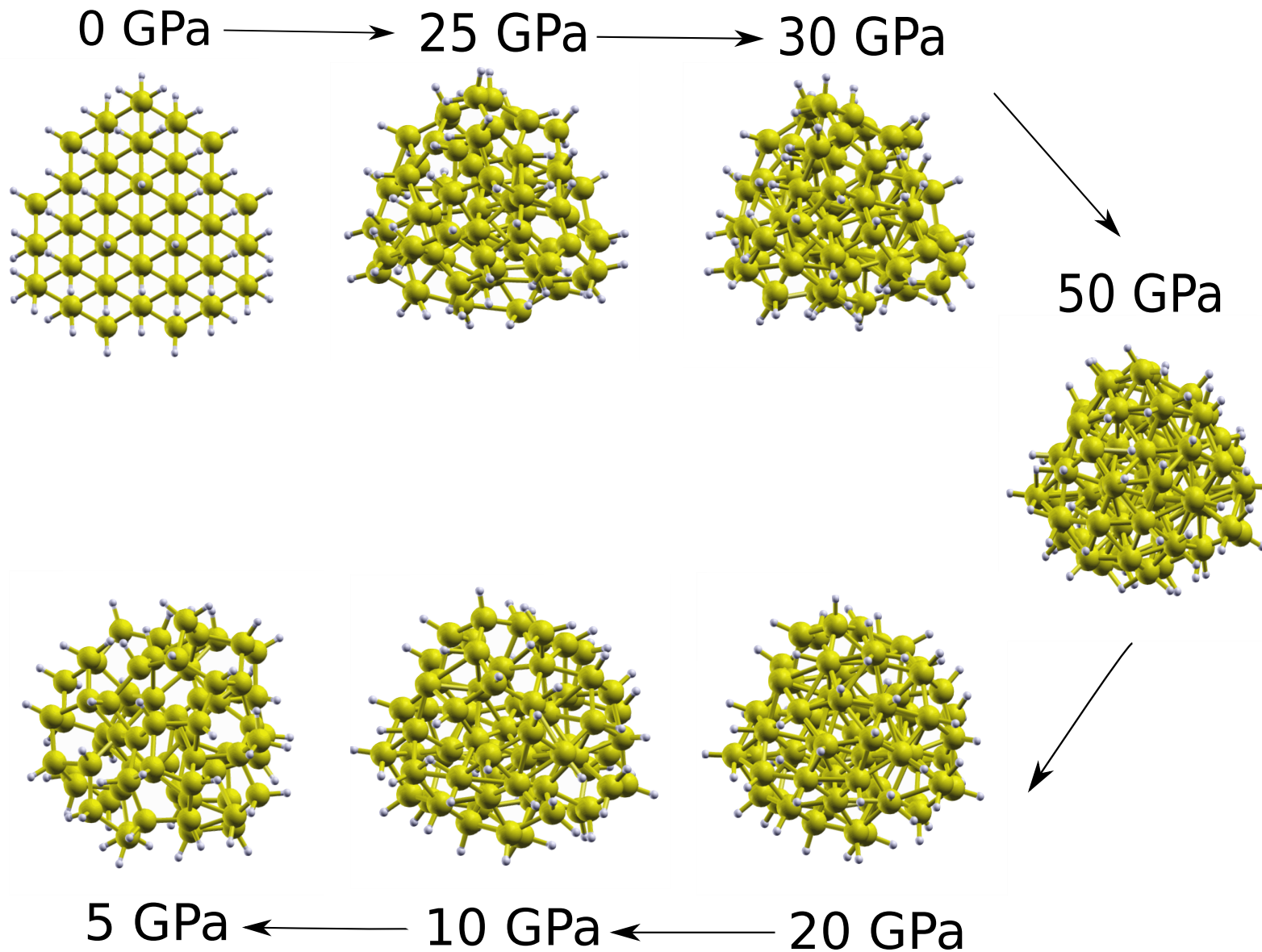
- Linear-scaling DFT<sup>2</sup> ([www.onetep.org](http://www.onetep.org))
- CAPZ LDA
- Norm-conserving pseudopotentials
- 800 eV cutoff
- Quasistatic geometry relaxation

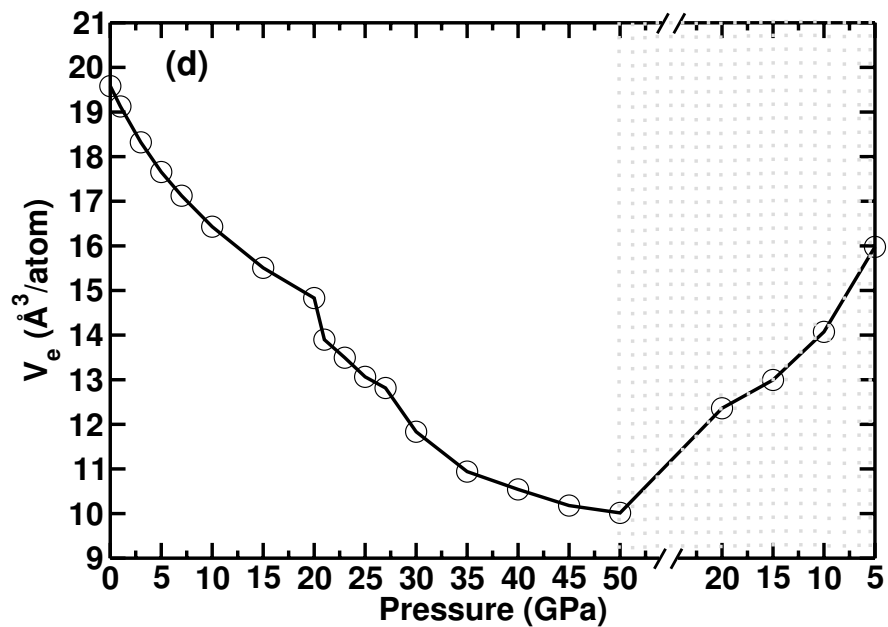
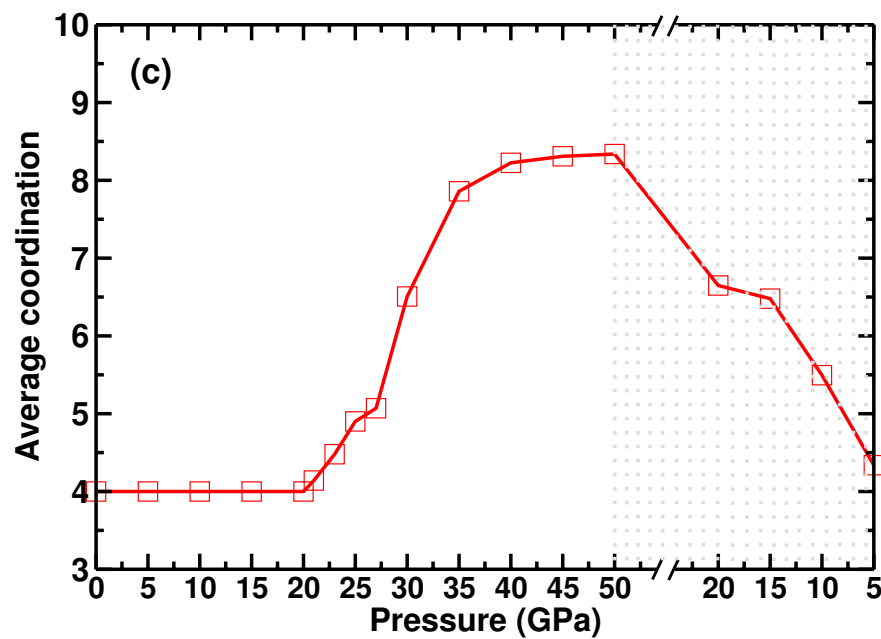
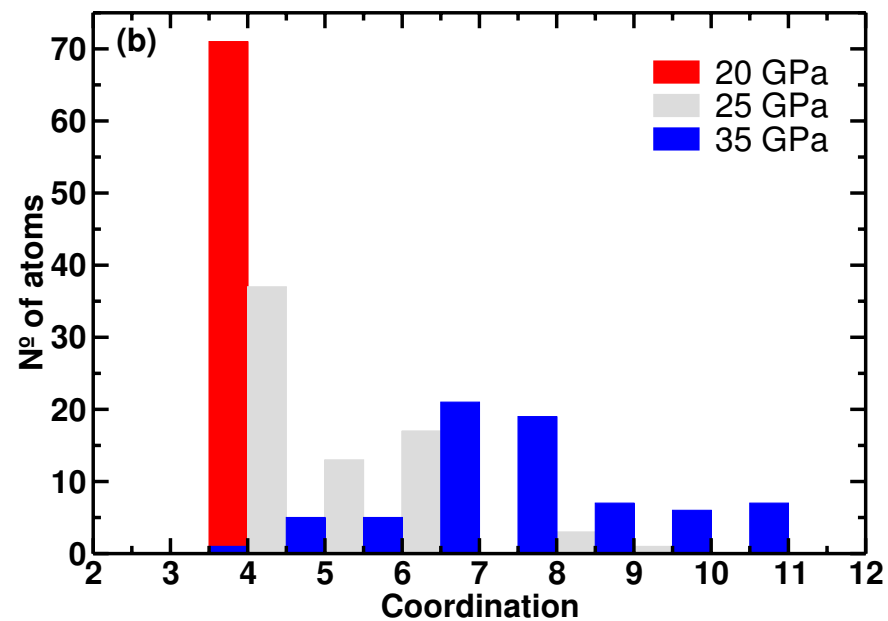
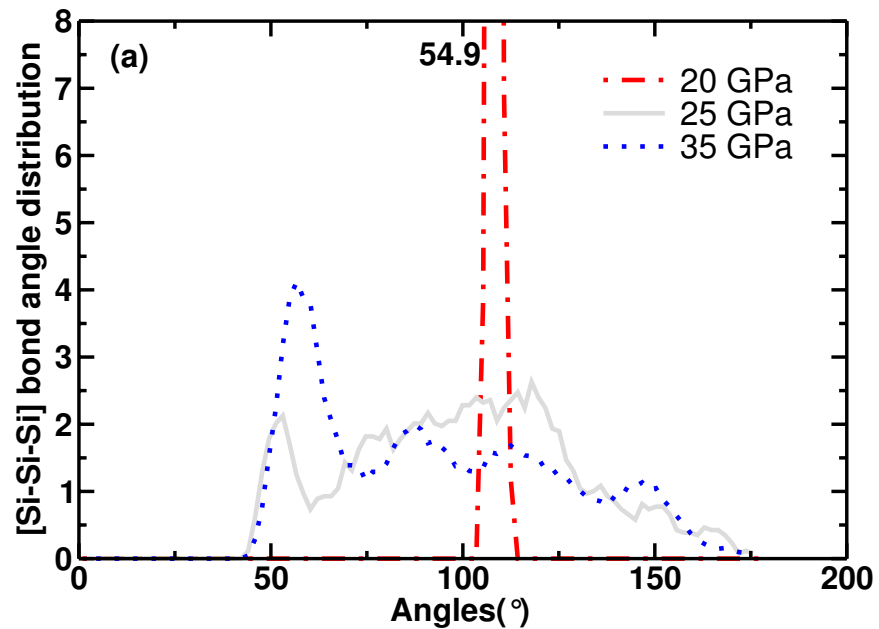


[1] Vinet et al, J. Phys. C: Solid State Phys. 19, L467 (1986)

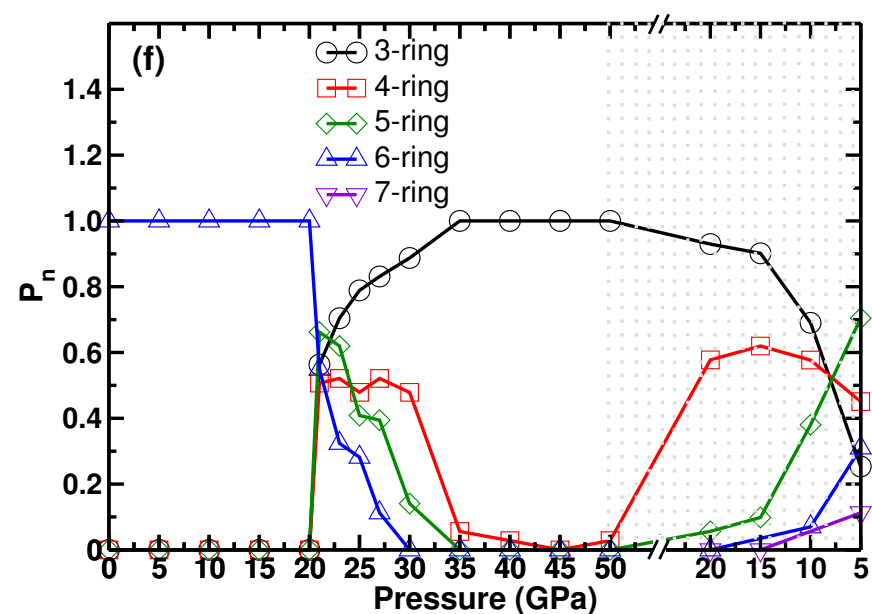
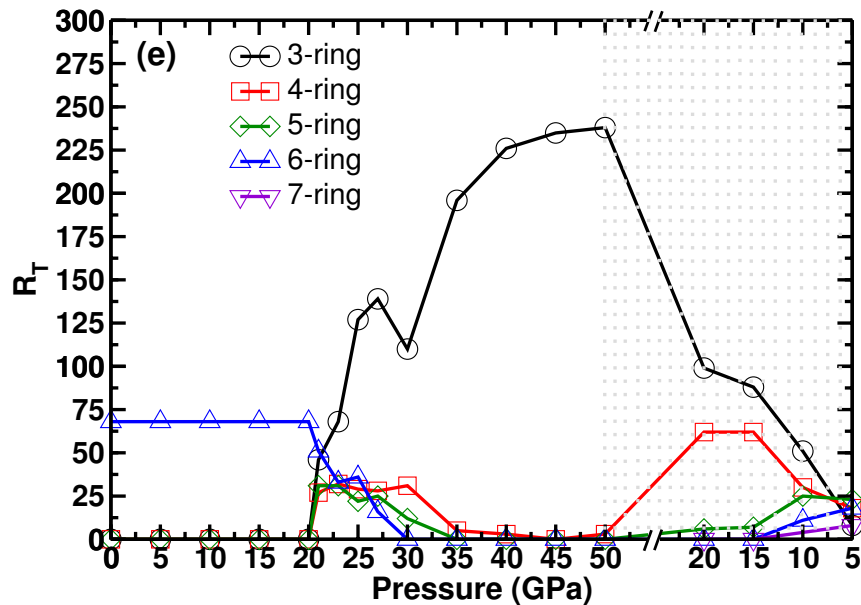
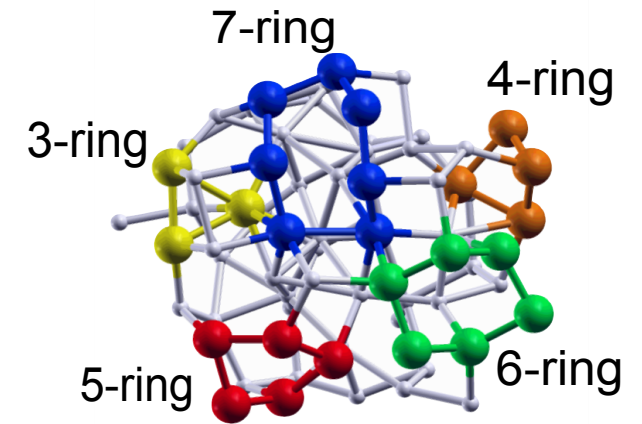
[2] Skylaris et al, J. Chem. Phys. 122, 084119 (2005)

# Pressure-induced amorphization



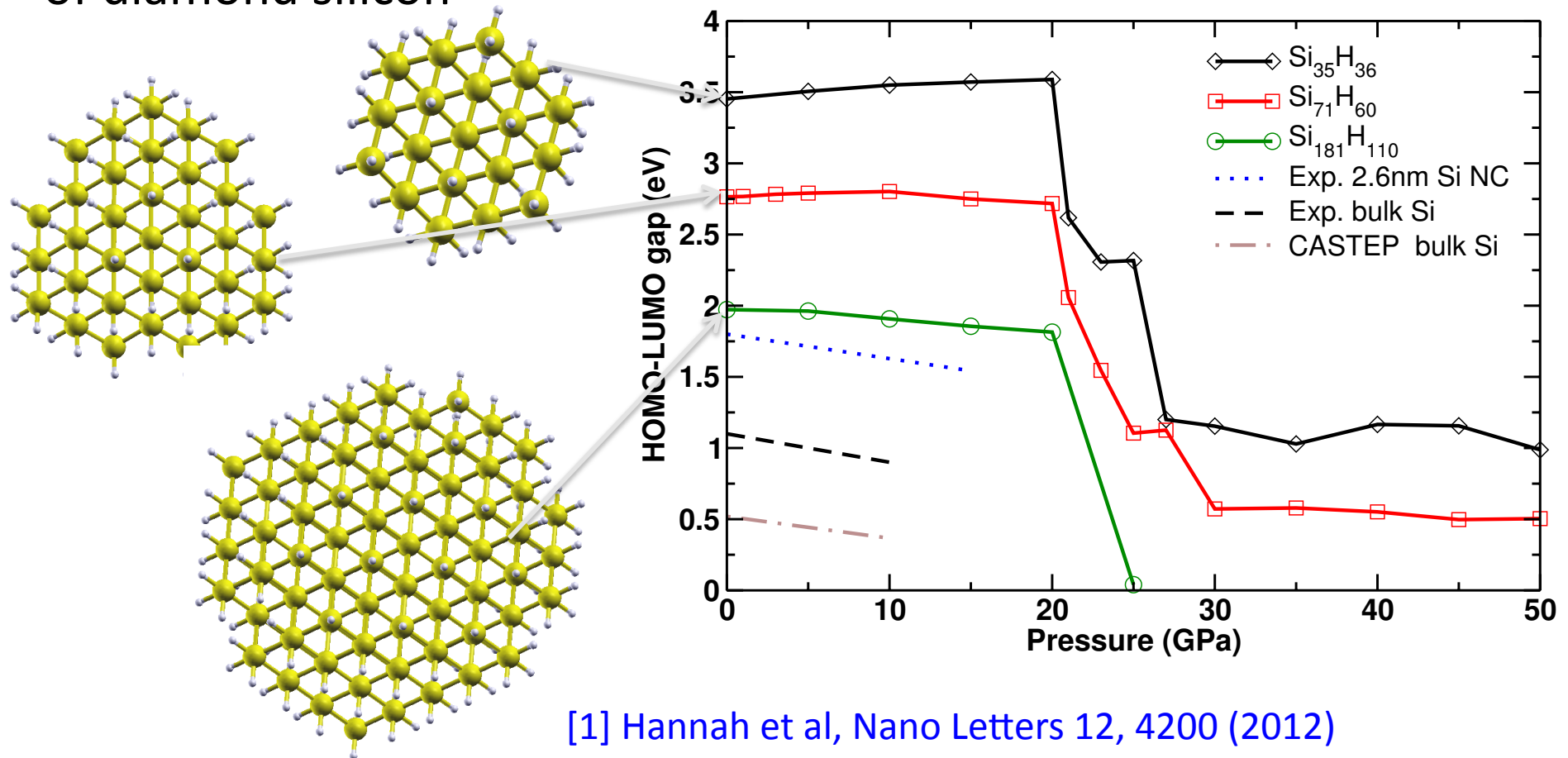


- Use ring statistics to track changes in covalent Si network
- **Polyamorphic transformations** between 3 types of amorphous structures: HDA, VHDA and LDA (upon decompression)
- **Consistent** with results obtained using **explicit solvents**



# Size-dependence

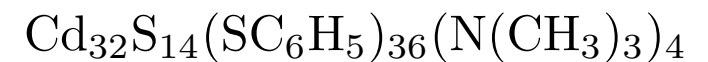
- Dramatic change of the HOMO-LUMO gap with pressure
- Qualitative agreement with experiment<sup>1</sup> for larger nanocrystal
- Competition between quantum confinement and pressure coefficient of diamond silicon



[1] Hannah et al, Nano Letters 12, 4200 (2012)

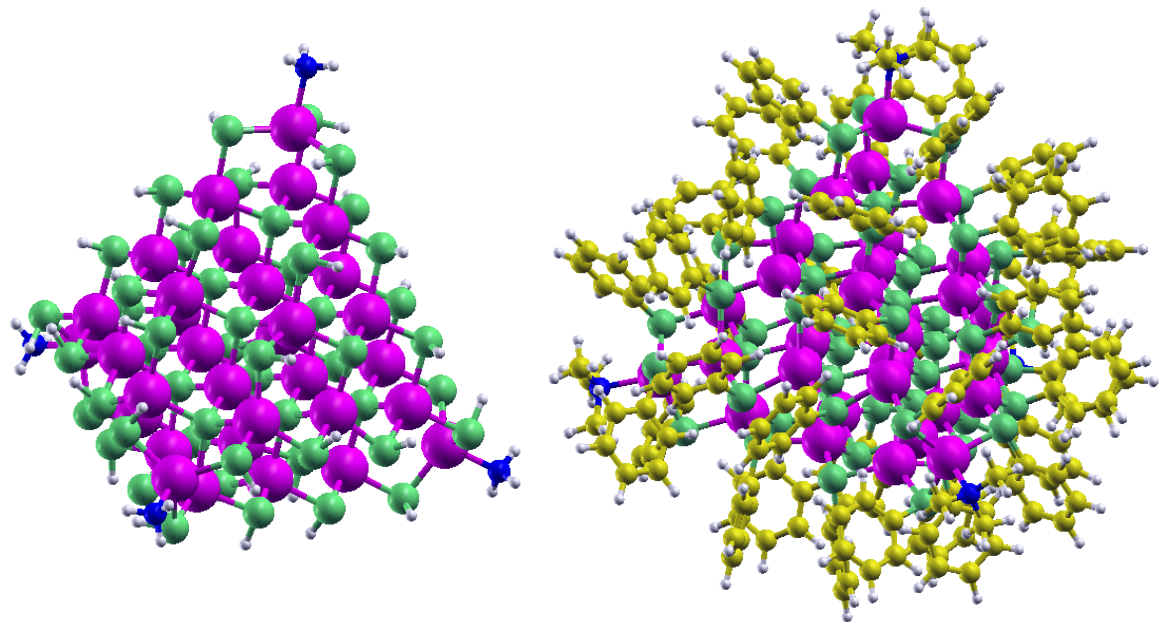
# II-VI pressure sensors?

- **CdS nanocrystals** with a zincblende core passivated with H and phenyl groups taken from experiment<sup>1</sup>
- Interested in the **effect of surfactants** on the structural and optical **properties under pressure**

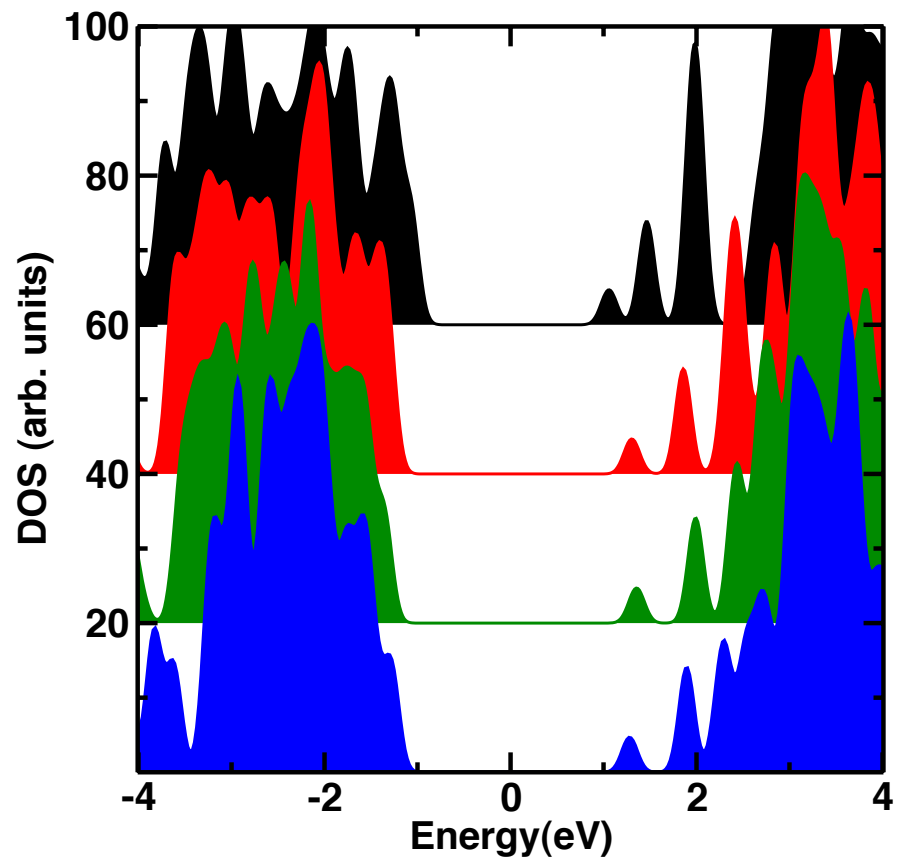
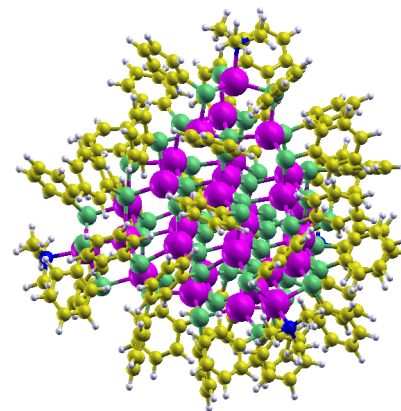
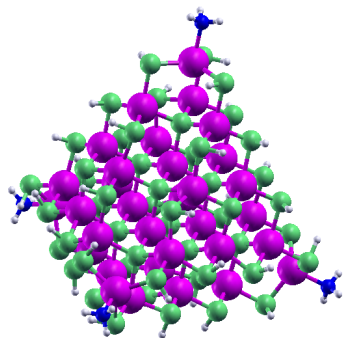


**SIMULATION DETAILS:**

- Blöchl PAW<sup>2</sup> in ONETEP
- PW92 LDA
- Scalar-rel. RRKJ projectors
- Extra 'd' partial wave for S
- 2 partial waves/ l channel
- 800 eV
- Quasistatic geometry relaxation



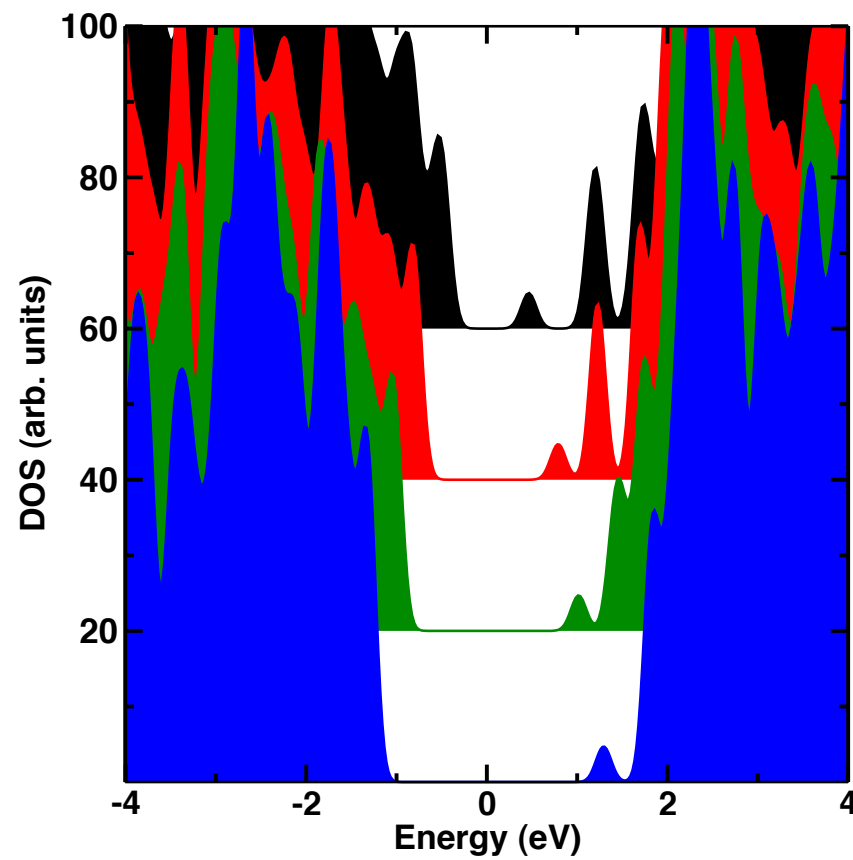
[1] Herron et al, Science 259(1993), 1426-1428; [2] Blöchl, Phys. Rev. B 50, 17953 (1994)



0 GPa



5 GPa

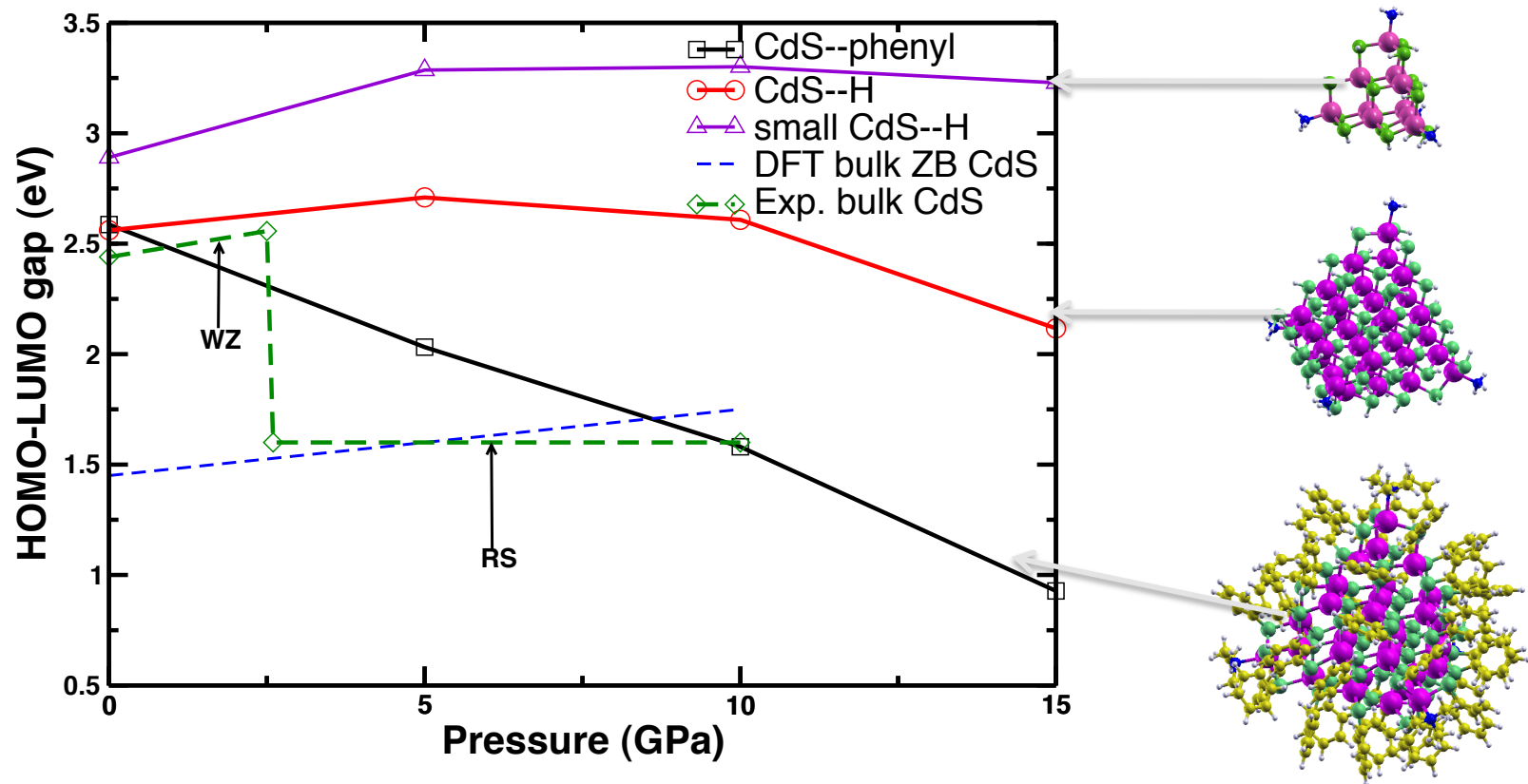


10 GPa



15 GPa



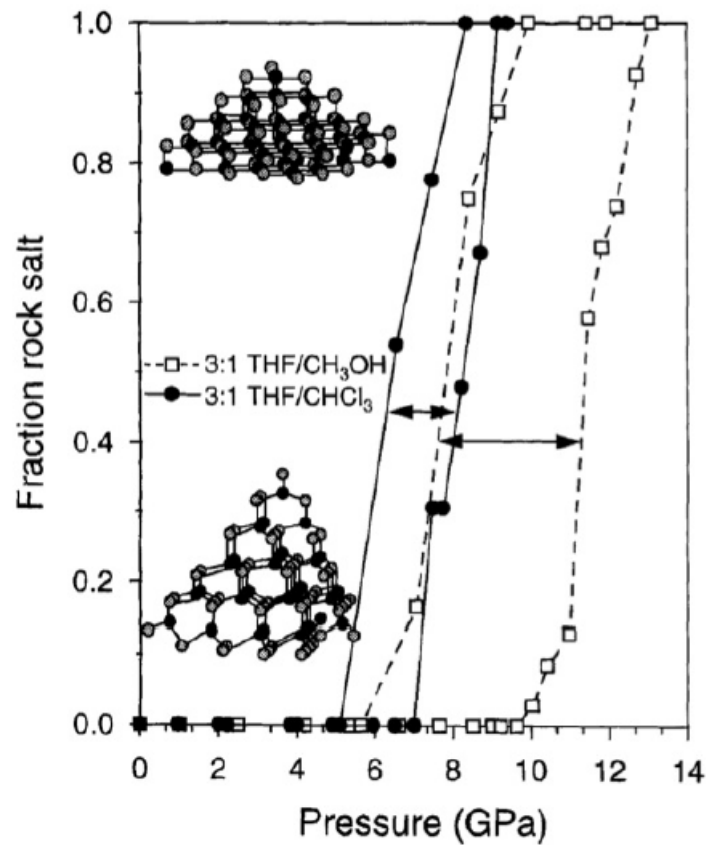


- Complex interplay between electronic and structural effects: quantum confinement, pressure coefficients, hybridization, surface distortions, ...
- Appearance of a mid-gap state (LUMO) due to the core
- Similar to CdSe but no consensus in the literature on origin

Puzder et al, PRL 92.21 (2004), 217401

# Work in progress

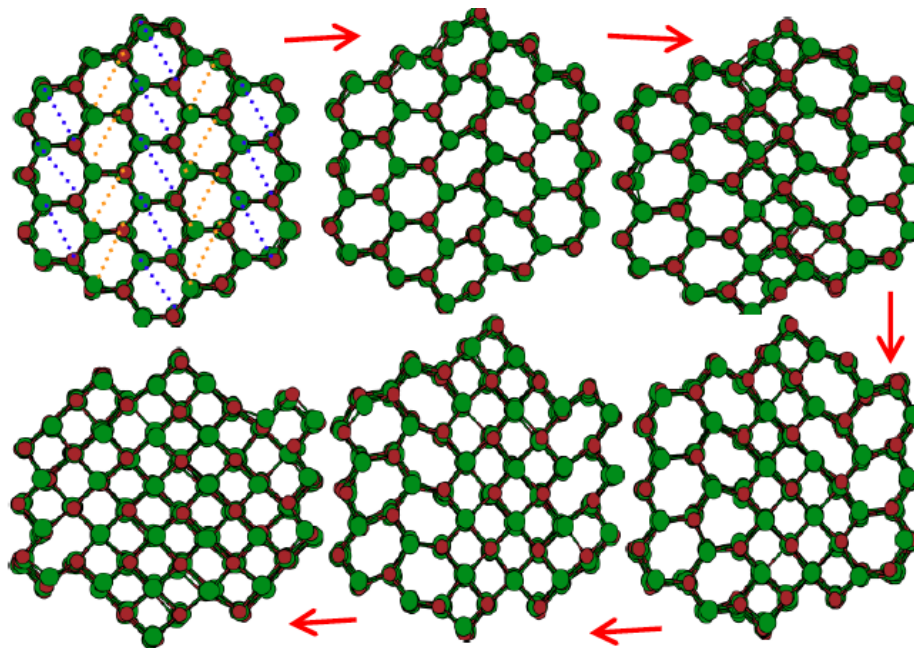
- Study kinetics of WZ/ZB  $\rightarrow$  RS transformation in nanocrystals
- Want to understand effect of surfactants and solvent on structural transformation



C. Chen, A. B. Herhold, C. S. Johnson, A. P. Alivisatos, Science 276, 398 (1997).

# Work in progress

- Long timescales involved too expensive for ab initio treatment
- Use classical MD combined with metadynamics to accelerate free energy landscape exploration
- Do ab initio calculations on MD snapshots



**Cd<sub>216</sub>S<sub>216</sub>**  
**P=1.75 GPa**  
**T= 300K**  
**w=5meV**  
**d=0.02**

# Summary

- Electronic enthalpy method is natural and efficient to simulate finite systems under pressure
- Need to calibrate terms defining the volume
- Gives similar results to explicit solvents
- Combined with linear-scaling DFT allows to investigate realistic nanocrystals under pressure
- Zincblende CdS nanocrystal is a candidate for pressure sensing
- Surfactants important in determining structural and optical response

# Acknowledgments

- Now available on [J. Chem. Phys. 139, 084117 \(2013\)](#)
- Collaborator: Andrea Greco
- Useful discussions: Francesco Mauri
- Funding: EPSRC grant #EPG036888/1
- Compute resources: Imperial HPC and HECToR
- ONETEP developers

Imperial College  
London



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